

IMAGE GUIDED TRANSORBITAL ENDOSCOPIC PROCEDURES

By

Nkiruka Atuegwu

Dissertation

Submitted to the Faculty of the
Graduate School of Vanderbilt University

In partial fulfillment of the requirements

For the degree of

DOCTOR OF PHILOSOPHY

In

Biomedical engineering

December 2008

Nashville, Tennessee

Approved:

Robert L. Galloway

Michael I. Miga

Louise A. Mawn

Alfred. B. Bonds

Jay. B. West

ACKNOWLEDGEMENTS

First of all, I will like to thank my advisor and mentor Dr Bob Galloway for his support, guidance and encouragement. This work and my PhD career will not have been possible without him.

I will like to thank my other committee members Dr Louise Mawn, Dr Michael Miga, Dr Jay West and Dr Alfred Bonds for all their help and advice throughout these years. I appreciate all the time, effort and input that all they have given me over the course of my research.

I will like to thank Dr Cari Lyle and Dr Lillian Ringsdorf for their help with data collection. I will also like to thank the Vanderbilt CT staff for all their help with image acquisition.

This work will not have been possible without the various members of the SNARL and BML lab (past and present). Thank you all for your input, assistance and friendship throughout these years.

To my friends and family, I appreciate all the love, support and encouragement you have given me and to my husband Emeka, I cannot thank you enough for always being there for me.

TABLE OF CONTENTS

	Page
ACKNOWLEDGEMENTS.....	III
TABLE OF CONTENTS.....	IV
LIST OF TABLES.....	VI
LIST OF FIGURES	VII
CHAPTER	
I. PURPOSE AND SPECIFIC AIMS.....	1
II. BACKGROUND.....	3
Endoscopy.....	3
Orbital Endoscopic Procedures.....	5
Image Guided Surgery and Interventions.....	12
<i>Registration</i>	13
<i>Localization and Tracking</i>	14
<i>Magnetic Tracker: Aurora</i>	15
Motivation for the specific aims.....	19
References.....	20
III. MANUSCRIPT 1- VOLUMETRIC CHARACTERIZATION OF THE AURORA MAGNETIC TRACKER SYSTEM FOR IMAGE GUIDED TRANSORBITAL ENDOSCOPIC PROCEDURES.....	22
Abstract.....	22
Introduction.....	23
Materials and methods.....	28
Results.....	38
Discussion.....	45
References.....	47
IV. MANUSCRIPT 2- SENSITIVITY ANALYSIS OF FIDUCIAL PLACEMENT ON TRANSORBITAL TARGET REGISTRATION ERROR.....	49
Abstract.....	49
Introduction.....	50
Materials and Methods.....	52
Results.....	63
Discussion.....	71

References	72
V. MANUSCRIPT 3- IMAGE GUIDED TRANSORBITAL ENDOSCOPIC PROCEDURE IN PHANTOMS	74
Abstract	74
Introduction	75
Methods	80
Results	84
Discussion	89
Acknowledgement.....	89
References	90
VI. SUMMARY	92
APPENDIX	
A. ACCURACY MEASUREMENT OF THE EFFECT OF SOME MATERIALS ON THE AURORA MAGNETIC SYSTEM.....	94
B. DEALING WITH CORRELATED FILE	96

LIST OF TABLES

Table	Page
Effects of different substances on retinal damage caused by optic nerve injury, NMDA-induced toxicity or ischaemia [9]	10
The minimum and the maximum variances obtained for fiducials 1 and 121 and the number of points that correspond to the minimum and maximum values. Table also shows the variance calculated with 150 points.	33
Random FLE of both the 5D and the 6D sensors for a z value of 4cm	42
Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 4cm	42
Random FLE of both the 5D and the 6D sensors for a z value of 6cm	43
Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 6cm	43
Random FLE of both the 5D and the 6D sensors for a z value of 12cm	44
Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 12cm	44
The mean, standard deviation and the maximum values of the RMS distance of the localized fiducial points from the mean of the distances.	65
The accuracy and the time of image guided and non image guided endoscopic phantom studies	89
Errors and variances due to the different materials	95
Translational TRE values for the optimized fiducial configuration	99
Translational TRE values for the unoptimized fiducial configuration	99

LIST OF FIGURES

Figure	Page
Picture of a flexible endoscope. [http://en.wikipedia.org/wiki/Endoscopy].....	4
Schematic of the optic nerve within the retrobulbar space [http://www.wetcanvas.com].....	6
The Aurora magnetic tracker system from NDI[http://www.ndigital.com/]	16
Schematic of the metal and field source and sensor distance	18
Diagram of the Aurora magnetic tracker. A is the field generator and B is the sensor	25
Schematic and setup of the grid used for the measurement. A shows grid measurements and B shows the setup for the data collection.	30
Variance calculated for fiducial 1 and 121 using 50 to 1000 points. The asterisks represent fiducial 1 and circles represent fiducial 121.	32
Schematic of the volumetric movement of the measurement grid for the endoscopic procedure.	34
Schematic of the different possible positions of the Aurora system. The dark gray orbital region shows the orbit of interest	36
The schematic of the orbital triangle formed for position A in Figure 9.....	37
Graph of the random FLE of a sample plane (plane 2) intersecting the magnetic field. Figure on the left is the 6D and the figure on the right is the 5D.....	39
Figure showing the relative spatial error of a sample plane (plane 5) intersecting the magnetic field. The figure on the left shows the error for the 6D and the figure on the right shows the error for the 5D tracker.	40
Cartoon of the target region. The <i>stars</i> show the target region and some of the possible locations of the target.	58
Picture of the face with the skin fiducials and the LADS with reference frame attached.	61

a) Skull phantom with the initial and final fiducial positions. The squares are the initial fiducial position and the circles are the final fiducial position. b) Laser range scan of the skull phantom with the taboo regions.	64
TRE calculated in the target region for FLE value of 1mm for an initial naïve initial fiducial position.....	67
TRE calculated in the target region for FLE value of 4mm for an initial naïve initial fiducial position.....	68
Average TRE in the target region for ten different simulations of the simulated annealing program.....	70
Picture of the possible placements of the magnetic tracker[13]	79
Picture of the experimental setup.....	81
Screen shot of the ORION image guidance software used. The three planes show the three orthogonal views of the skull phantom and the last plane shows the endoscopic view.	83
Graph of the non image guided times vs. the image guided times for the different targets for the attending surgeon. The line represents the times when the time to target with image guidance was equal to the time to target with non image guidance.	85
Graph of the non image guided times vs. the image guided times for the different targets for the surgical fellow.....	87
Graph of the non image guided times vs. the image guided times for the different targets for the surgical resident.	88
The possible placements of the Aurora magnetic tracker relative to the head.	97
Overlay of the skull phantom and the grid phantom.....	98
Planar overlay of the grid phantom and skull phantom	98

CHAPTER I

PURPOSE AND SPECIFIC AIMS

Endoscopic orbital procedures are hindered by both the difficulty in differentiating between orbital structures and the loss of orbital landmarks during these procedures. These difficulties are due to the orbital fat that obstructs direct vision of the orbital structures. Image guidance can address these problems because real time image and physical space tracking information can be provided to the surgeons during the orbital procedure to help in the delivery of therapy to the orbit.

The research plan proposes to study the feasibility of image guided endoscopic orbital procedures. Specifically this research will:

Specific Aim 1: *Characterize the magnetic tracking system.*

- The volumetric random and the spatially dependent fiducial localization error will be characterized.
- The accuracy of the sensor measurements in the presence of a flexible endoscope will be characterized.

Specific Aim 2: *Determining an optimal fiducial placement that minimizes TRE in a target zone.*

- The optimal fiducial placement to minimize the TRE of the optic nerve eye junction will be determined.
- Sensitivity analysis will be performed on the fiducials to determine the effect of random errors in fiducial placement on TRE.

- Skin motion experiments will be carried out to give an estimate of the FLE due to skin motion that can be expected.

Specific Aim 3: *Validation of the possibility of image guidance to the optic nerve.*

- Image guided endoscopic orbital procedure will be compared to non image guided endoscopic procedures using phantoms. The timing and targeting comparisons will be used as a measure of the advantage and the possibility of image guided orbital endoscopic procedures.

CHAPTER II

BACKGROUND

Endoscopy

Endoscopy is the examination and inspection of the interior of body organs, joints or cavities through an endoscope inserted into the body through a natural or created aperture. It is a minimally invasive procedure. An endoscope consists of a rigid or flexible tube and a light delivery system to illuminate the organ or object under inspection. An endoscope uses two fiber optic lines. A "light fiber" carries light into the body cavity and an "image fiber" carries the image of the body cavity back to the physician's viewing lens. There is also a separate port to allow for administration of drugs, suction, and irrigation. This port may also be used to introduce small folding instruments such as forceps and scissors for tissue excision, sampling, or other diagnostic and therapeutic work. Figure 1 is a picture of a flexible endoscope. Endoscopes can be used for a variety of medical procedures such as bronchoscopy, gastroscopy and endoscopic biopsy. Of importance to this work is the use of endoscopes for orbital procedures.

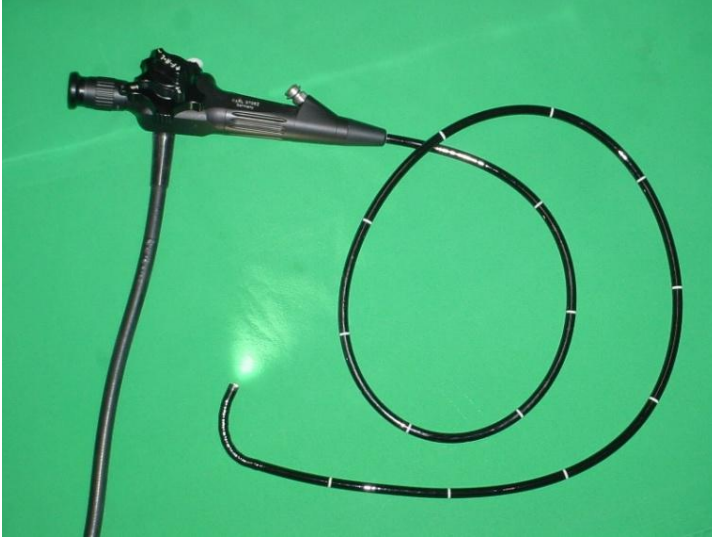


Figure 1: Picture of a flexible endoscope. [<http://en.wikipedia.org/wiki/Endoscopy>]

Orbital Endoscopic Procedures

The optic nerve's location behind the globe in the intraconal space (Figure 2) makes open surgical access available only to highly trained orbital surgeons. Access to the retrobulbar optic nerve has traditionally required an orbitotomy; an invasive procedure in which either a rectus muscle is dissected from the globe or the lateral bony wall of the orbit removed. It is not practical to perform complex, invasive orbital surgery for the large numbers of individuals suffering from optic nerve disease. The use of endoscopes can reduce this invasiveness.

Endoscopes were first used by Norris and Cleasby in the late 1970's for orbital surgery and later for orbital biopsies. They made an initial attempt at guidance with a stereotaxic positioner to hold the endoscope at a fixed position but they had great difficulty with the stereotaxic arm and discontinued use [1-3]. Since then various attempts at using the endoscope in the orbit have been reported.

Recently, Mawn et al used a flexible endoscope to navigate the orbit for optic nerve sheath fenestration (ONSF). They reported that there were problems with navigation through the orbit because the orbital structures were of similar color and also because the traditional orbital landmarks were lost as the endoscope was moved through the orbit. They also reported that it took as much as 3 hours to complete an ONSF in a human cadaver [4].

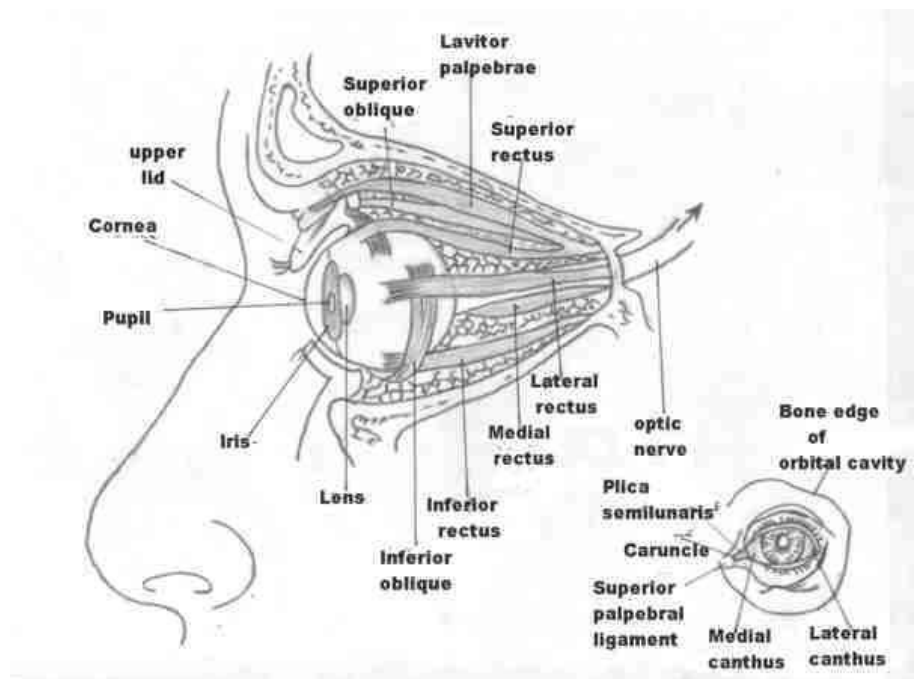


Figure 2: Schematic of the optic nerve within the retrobulbar space [<http://www.wetcanvas.com>]

Potential Orbital Endoscopic Procedures

New research on neuroprotection has brought into the light other potential uses of endoscope. Neuroprotection is the strategy of treating a disease by preventing neuronal death. Neuroprotection is useful even when the exact cause of a disorder is undefined, as the therapy occurs at the level of the dying cells and not at the initial site of injury.

Optic neuropathies, a group of diseases characterized by visual loss due to optic nerve dysfunction are one of the main targets of neuroprotective therapy. The most common optic neuropathy is that associated with glaucoma. Glaucoma in general results in changes in the trabecular meshwork of the eye. Primary Open-Angle Glaucoma (POAG) and Primary Angle-Closure Glaucoma (PACG) are characterized by damage to the optic nerve, retinal ganglion cell death and visual field loss which include the loss of peripheral vision, depth perception, and contrast sensitivity [5]. The optic nerve damage is thought to occur in the optic nerve head [6]. The number of people with primary glaucoma in the world in 2000 was estimated at nearly 66.8 million, with 6.7 million suffering from bilateral blindness [7]. It is estimated that there will be 60.5 million people with primary open-angle glaucoma (POAG) and primary angle-closure glaucoma (PACG) in 2010, increasing to 79.6 million by 2020. Bilateral blindness will be present in 4.5 million people with POAG and 3.9 million people with PACG in 2010, rising to 5.9 and 5.3 million people in 2020, respectively [8].

A wide variety of other optic neuropathies also cause visual loss, e.g. inflammatory, ischemic, infiltrative, and traumatic optic neuropathies. A number of factors can be responsible for the disease, but in all types of optic neuropathy, the injury is manifested at the optic nerve axon and results in the loss of retinal ganglion cells (RGCs) through apoptosis [9].

Several neuroprotective strategies may be useful for preventing retinal ganglion cell death after axonal injury. These include delivery of neurotrophins, blockade of receptors mediating excitotoxicity, and scavenging of reactive oxygen species [6].

Table 1 depicts pharmacological agents that affect the RGC cells that are damaged due to optic nerve transection, NMDA- induced toxicity and ischemia. NMDA is an amino acid derivate that acts as an agonist at an NMDA receptor.

While neuroprotective drugs are developed and tested, there is a need to effectively deliver the drugs to the optic nerve especially to the axon [10].

Table 1: Effects of different substances on retinal damage caused by optic nerve injury, NMDA-induced toxicity or ischaemia [9]

Substances	Optic nerve injury	NMDA	Ischaemia
α_2 -Adrenoceptor agonists	Protective	Unknown	Protective
BDNF	Protective	Protective	Protective
CNTF	Protective	Protective	Protective
bFGF	Protective	Unknown	Protective
Caspase-1 inhibitors	Not protective	Protective	Protective
Caspase-3 inhibitors	Protective	Unknown	Protective
NMDA antagonists	Protective	Protective	Protective

Current Methods of Ocular Drug Delivery

Topical administration of medications is the easiest method for drug delivery to the eye but the disadvantage of this method is that topical delivery often fails to provide therapeutic levels in the vitreous cavity or posterior segment because at least 80% of the applied medication disappears via lacrimal drainage and does not enter the eye [11]. Other factors that hinder the movement of the drug to the posterior regions include aqueous production, blood flow, and barriers imposed by the corneal epithelium and endothelium and by the stromal tissues of the cornea and sclera [12]. This makes topical administration of drugs an inadequate method for the treatment of vitreoretinal diseases [13].

Transdermal therapeutic systems have been proposed for ocular drug delivery but they only have a slight increase in concentration of the drug in the posterior segment when compared to the topical drug delivery and, as such, are inadequate for treatment of posterior optical neuropathies [12].

Drugs can often be delivered to the posterior segment by injection via the pars plana. However, depending on the rate of clearance from the vitreous of a particular medication, large boluses and frequent administrations may be required to ensure therapeutic levels over an extended period of time. Multiple intraocular injections can lead to an increased likelihood of complications, such as vitreous hemorrhage, retinal detachment, and endophthalmitis [13].

Intravitreal implants of sustained release drugs that provide constant levels of drug to the eye have been used. The disadvantage of this is that drugs that are safe to the eye when used for a short time may prove to be toxic when allowed to maintain long standing intraocular levels. There are also risks associated with the surgical placement of intravitreal implants. These include vitreous hemorrhage, retinal detachment, and endophthalmitis [13]. Furthermore, not all the

drugs can be developed into an implant because an implant requires a coating material that does not react to the drug and allows a sustained release of the drug. The feasibility of the use of the intravitreal implants is limited in cases of trauma and damage to the vitreous of the eye where an implant may not be feasible. In trauma cases, the need for immediate protection of RGCs before additional surgery precludes the use of implants for immediate protection of the RGCs.

Most of the common methods of ocular drug deliveries do not effectively get the drugs to the optic nerve axon and may have additional side effects. A system that can guide an endoscope to the optic nerve for drug delivery can potentially be used for delivery of neuroprotective drugs to the optic nerve cells.

For orbital endoscopic procedures to be used, the problem of navigation through the orbital fat has to be improved since the orbital fat obscures easy visualization of optic nerve during localization. This can be solved by the use of image guidance during the endoscopic procedure.

Image Guided Surgery and Interventions

Image guided surgery and interventions involve the use of medical images to select, plan and guide a surgical procedure or medical intervention. Because of the accuracy that image-guided surgical technology provides, surgeons are able to create an exact, detailed plan for the surgery and the intervention — where the best spot is to make the incision, the optimal path to the targeted area, and what critical structures must be avoided. The real-time feedback provided by the computer helps surgeons make adjustments to ensure they are exactly treating the desired areas.

Image guided surgery is based upon integration of the preoperatively acquired and processed information such as an image volume of the patient and the corresponding anatomy of

the patient within the same frame of reference. The images can be projective images such as plane films and angiograms; tomographic sets such as computed tomography (CT), magnetic resonance imaging, (MRI), single-photon emission computed tomography (SPECT), positron emission tomography (PET) and Functional MRI (fMRI). It can also include intraoperative two-dimensional imaging such as ultrasound images, laparoscopic, endoscopic and microscopic images. Links between these two components are realized by combining image-to-patient registration and by tracking instruments within the operating field.

Registration

Registration can be defined as the determination of a one to one mapping between the coordinates in one space and those in another, such that the points in the two spaces that correspond to the same anatomic structure are mapped together. Image-based registration can be divided into extrinsic and intrinsic methods [14]. Intrinsic methods rely on patient-generated image content. Extrinsic methods rely on artificial objects attached to the patient. These objects are designed to be well visible and accurately detectable in all of the relevant modalities. The point derived from the intrinsic or extrinsic object used for registration is called a fiducial point and the extrinsic object which contains the fiducial point is called a fiducial marker.

Two basic types of fiducial markers are used in neurosurgical IGS: bone implantable markers [15] and skin surface fiducials [16]. Bone implanted fiducials generally are more invasive and cannot be used for procedures that are repetitively done on a patient. Skin fiducials are not invasive and can be used frequently on a patient. Since skin moves over the bone, skin fiducials are by nature, more mobile than bone implantable markers, and this may lead to an increase in the localization error of the skin fiducials. This increase in localization error leads to an increase in TRE during the IGS procedure.

The quality of fiducial-based registration may be judged by several types of registration error computed after the registration. The three main measures of registration are Fiducial localization Error (FLE), Fiducial Registration Error (FRE) and Target Registration Error (TRE). FLE is the error in locating the position of a fiducial. FRE is the distance between corresponding fiducial points after registration. TRE is the distance between the corresponding “target” points after registration. “Target” in this case means points other than the fiducial points. [17].

Some of the factors that contribute to the FLE are the accuracy of localization of a fiducial by the tracking system, the signal to noise ratio of the image, the imaging markers used and image distortion [17].

TRE is affected by both the FLE of the system and the placement of fiducials[18].

$$\langle TRE^2 \rangle = \langle FLE^2 \rangle \left(\frac{1}{N} + \frac{1}{K} \sum_{i=1}^K \sum_{j \neq i}^K \frac{r_i^2}{\Lambda_{ii}^2 + \Lambda_{jj}^2} \right) \quad 1$$

N = Number of fiducials

K = Spatial dimension; $K=3$

r_i = Distance between the centroid of the fiducials and the target

Λ =Eigenvalues of the fiducial arrangement

From equation 1, it can be observed that minimizing the error due to the placement of the fiducials can lead to a decrease in the TRE observed especially in the cases when the FLE cannot be minimized further. After registration is carried out, the surgical or interventional instruments have to be tracked within the operational field.

Localization and Tracking

Physical space localization methods are used to track the three-dimensional position of surgical instruments, digitize points and surfaces on the anatomy, and provide links between

preoperative image studies and any available intraoperative data. Localizers used for image guided procedures can be reduced to two classes of devices: geometric and triangulation.

Geometric localizers use angle, extension, and/or bend systems to sense the position of the procedural device. In triangulation, an emitter or emitters broadcast energy, or a reflector or reflectors return energy, to a series of detectors at known locations. This is used to calculate the position and orientation of the emitter. Triangulation systems can be ultrasonic, optical or magnetic [19].

Optical and ultrasonic trackers are line-of-sight devices; a free optical path between sensor assembly and emitter is necessary in order to acquire data. This makes optical tracking systems unsuitable for the tracking of flexible endoscopes or other instruments in the body; optical trackers cannot be embedded in instruments that are completely inserted in the body: because a line of sight has to be maintained between the markers and the optical localizer system. Magnetic trackers, however, do not have a line of sight problem and can be used to track instruments within the body. For this reason, we choose to use a magnetic tracking system to perform the physical space localization in this work.

Magnetic Tracker: Aurora

The Aurora system (Northern Digital Inc, Waterloo, Ontario) is an alternating current (AC) magnetic localizer system which emits AC magnetic fields at a maximum of 40 Hz. It consists of a field generator (right hand side of Figure 3), a control unit (left hand side of Figure 3), and small coil sensors that can be embedded in catheters, endoscopes, and other instruments.



Figure 3: The Aurora magnetic tracker system from NDI[<http://www.ndigital.com/>]

The Aurora field generator unit contains coils that generate electromagnetic field. When a tracked tool is placed inside the magnetic field, voltages are induced in the sensor coils that are embedded in the tools. The induced voltage is then used to calculate the position and orientation with five or six degrees of freedom (x, y, z translations and two or three orientations) of the sensor coils. As the magnetic fields are of low field strength and can safely pass through human tissue, location measurement of an object is possible without the line-of-sight constraints of an optical spatial measurement system.

The disadvantage of magnetic localizers is that they induce eddy currents in nearby conductive materials. These eddy currents induce secondary magnetic fields that change the induced voltages measured by the sensors. This change in induced voltage leads to systematic tracking errors. The Aurora system attempts to minimize these deviations through an iterative algorithm for position and orientation calculation but some changes in induced voltage in the sensors are still observed.

Several groups have studied the effect of metallic materials on the accuracy of a magnetic tracker. In theory, the error in the calculated position due to a metal object Δr is predicted to be [20, 21]

$$\Delta r \propto \frac{d_{tr}^4}{d_{tm}^3 d_{mr}^3} \quad 2$$

Where: d_{tr} is the distance between the field source (transmitter) and the sensor (receiver), d_{tm} the distance between the field source (transmitter) and the metal and d_{mr} the distance between the metal and the sensor (receiver).

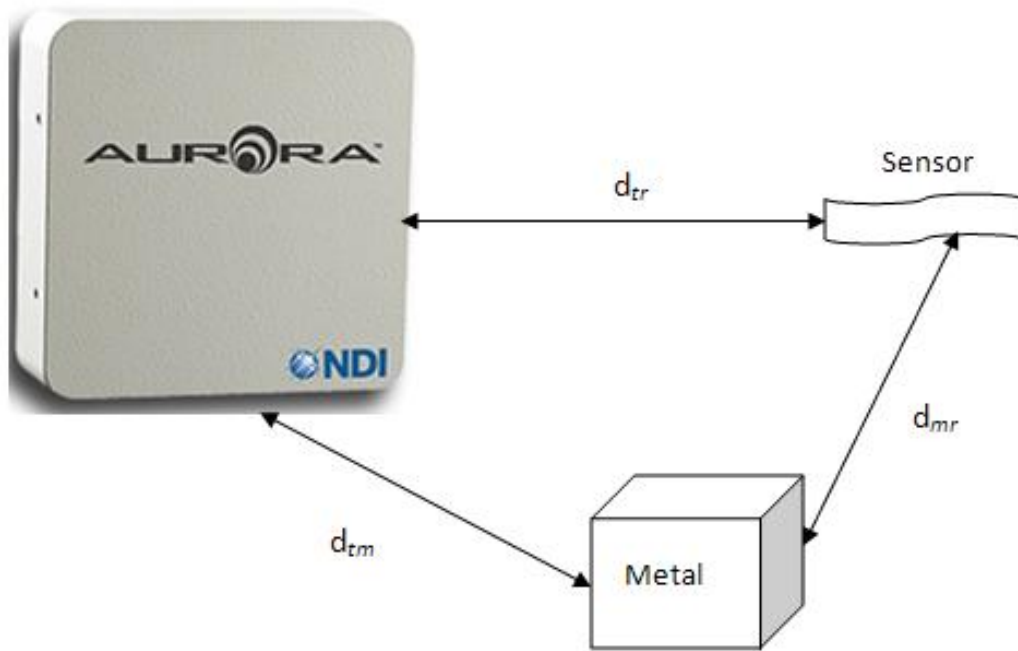


Figure 4: Schematic of the metal and field source and sensor distance

From the above equation, it can be seen that the error in localizing a point decreases as the metal-transmitter and metal-receiver distances are increased. This indicates that while metals in the work volume lead to incorrect sensor readings, careful placement of the transmitter and the sensor in relation to the metals in the environment can help reduce the amount of error in the measured position of the sensor.

Motivation for the specific aims

Image guidance requires an image-space to physical-space registration and tracking in physical-space with a localizer. To effectively use a magnetic localizer for transorbital guidance, the error metrics must be characterized so that expected guidance errors can be determined. Characterizing and understanding some of the tracking errors of the magnetic tracker will also help determine the best use of the tracker; the positional placement and the expected errors in any given location from the tracker. Working in the “sweet spot” of the magnetic tracker will help reduce the FLE experienced during the image guidance procedure.

After characterizing the magnetic tracker, the registration of the physical-space to image-space needs to be addressed. Since the target in this research is the optic nerve, a structure which can be anywhere in the retroorbital pyramid, a new form of fiducial placement is created. In this method the retroorbital pyramid was sampled and a fiducial placement which minimized TRE throughout the possible location of the optic nerve head was determined.

After characterizing the magnetic localizer and determining an optimal fiducial placement for the task of optic nerve drug delivery, the performance of the system had to be tested. An experimental protocol which allowed performance quantification in an application mimicking manner was developed. Performance metrics from that protocol were gathered on a number of surgeons.

References

1. Norris JL, C.G., *An endoscope for ophthalmology*. American Journal of Ophthalmology, 1978. **85**(3): p. 420-2.
2. Norris JL, S.W., *Bimanual endoscopic Orbital Biopsy*. Ophtalmology, 1985. **92**(1): p. 34-38.
3. Norris JL, C.G., *Endoscopic orbital surgery*. American Journal of Ophthalmology, 1981. **91**(2): p. 249-252.
4. Mawn, L.A.S., Jin-Hui ; Jordan, David R.; Joos, Karen M. , *Development of an Orbital Endoscope for Use with the Free Electron Laser*. Ophthalmic Plastic & Reconstructive Surgery, 2004. **20**(2): p. 150-157.
5. Coleman, A.L., *Glaucoma*. The Lancet, 1999. **354**(9192): p. 1803.
6. Levin, L.A., *Direct and Indirect Approaches to Neuroprotective Therapy of Glaucomatous Optic Neuropathy*. Survey of Ophthalmology, 1999. **43**(Supplement 1): p. S98.
7. Quigley, H.A., *Number of people with glaucoma worldwide*. British Journal of Ophthalmology, 1996. **80**(5): p. 389.
8. Quigley, H.A. and A.T. Broman, *The number of people with glaucoma worldwide in 2010 and 2020*. Br J Ophthalmol, 2006. **90**(3): p. 262-267.
9. N Osborne, G.C., C J Layton, J P M Wood, R J Casson and J Melena, *Optic nerve and neuroprotection strategies*. Eye, 2004. **18**: p. 1075-1084.
10. Jeffrey, G., *How does an axon grow?* Genes and Development, 2003. **17**: p. 941-958.
11. Lux, A., et al., *A comparative bioavailability study of three conventional eye drops versus a single lyophilisate*. Br J Ophthalmol, 2003. **87**(4): p. 436-440.
12. Myles, M.E., D.M. Neumann, and J.M. Hill, *Recent progress in ocular drug delivery for posterior segment disease: Emphasis on transscleral iontophoresis*. Advanced Drug Delivery Reviews, 2005. **57**(14): p. 2063.
13. Velez, G. and S.M. Whitcup, *New developments in sustained release drug delivery for the treatment of intraocular disease*. Br J Ophthalmol, 1999. **83**(11): p. 1225-1229.
14. Maintz, J.B.A. and M.A. Viergever, *A survey of medical image registration*. Medical Image Analysis, 1998. **2**(1): p. 1.
15. Maurer, C.R., Jr., et al., *Registration of head volume images using implantable fiducial markers*. IEEE Trans Med Imaging, 1997. **16**(4): p. 447-462.

16. Barnett, G.H., D.W. Miller, and J. Weisenberger, *Frameless stereotaxy with scalp-applied fiducial markers for brain biopsy procedures: experience in 218 cases*. Journal of Neurosurgery, 1999. **91**(4): p. 569-576.
17. West, J.B., et al., *Fiducial Point Placement and the Accuracy of Point-based, Rigid Body Registration*. Neurosurgery, 2001. **48**(4): p. 810-817.
18. Fitzpatrick, J.M., J.B. West, and C.R. Maurer, Jr., *Predicting error in rigid-body point-based registration*. Medical Imaging, IEEE Transactions on, 1998. **17**(5): p. 694.
19. Galloway, R.L., *The Process and Development of Image-guided Procedures*. Annual Review of Biomedical Engineering, 2001. **3**(1): p. 83-108.
20. Hummel, J.B., et al., *Design and application of an assessment protocol for electromagnetic tracking systems*. Medical Physics, 2005. **32**(7): p. 2371-2379.
21. Mark A. Nixon, B.C.M., W. Richard Fright and N. Brent Price *The Effect of Metals and Interfering Fields on Electromagnetic Trackers*. Presence, MIT Press, 1998. **7**(2): p. 204-218.

CHAPTER III

MANUSCRIPT 1- Volumetric characterization of the Aurora magnetic tracker system for image guided transorbital endoscopic procedures

Atuegwu N.C and Galloway R.L

Original form of manuscript appears in Phys. Med. Biol. 53 (2008) 4355-4368.

Abstract

In some medical procedures, it is difficult or impossible to maintain a line of sight for a guidance system. For such applications, people have begun to use electromagnetic trackers. Before a localizer can be effectively used for an image-guided procedure, a characterization of the localizer is required. The purpose of this work is to perform a volumetric characterization of the fiducial localization error (FLE) in the working volume of the Aurora magnetic tracker by sampling the magnetic field using a tomographic grid. Since the Aurora magnetic tracker will be used for image-guided transorbital procedures we chose a working volume that was close to the average size of the human head.

A Plexiglass grid phantom was constructed and used for the characterization of the Aurora magnetic tracker. A volumetric map of the magnetic space was performed by moving the flat Plexiglass phantom up in increments of 38.4 mm from 9.6 mm to 201.6 mm. The relative spatial and the random FLE were then calculated. Since the target of our endoscopic guidance is the orbital space behind the optic nerve, the maximum distance between the field generator and the sensor was calculated depending on the placement of the field generator from the skull.

For the different field generator placements we found the average random FLE to be less than 0.06 mm for the 6D probe and 0.2 mm for the 5D probe. We also observed an average relative spatial FLE of less than 0.7 mm for the 6D probe and 1.3 mm for the 5D probe. We

observed that the error increased as the distance between the field generator and the sensor increased. We also observed a minimum error occurring between 48 mm and 86 mm from the base of the tracker.

Introduction

The use of electromagnetic trackers for image-guided procedures has increased in popularity in recent years [1-3]. This can be attributed to newer generations of electromagnetic trackers that show both an increased accuracy and have a reduced sensor size [4] making them easier to embed in instruments. Optical trackers, which are the most commonly used localizers for image guidance, are line of-sight devices requiring a free optical path between the sensor assembly and the tracked tool. The need for a line of sight makes optical tracking systems unsuitable for instruments that are completely inserted into the body. Magnetic trackers on the other hand do not require a line of sight because magnetic fields can pass through the body. This makes magnetic trackers suitable for tracking flexible medical instruments such as endoscopes. Since our lab is working on image-guided transorbital endoscopic procedures we chose to use an Aurora magnetic tracking system for the image-guided procedure. The Aurora system (Northern Digital Inc, Waterloo, Ontario) is an alternating current (ac) magnetic localizer system which emits ac magnetic fields. It consists of a field generator (A) and a small coil sensor that can be embedded in catheters, needles and other instruments (B). This is shown in Figure 5. The Aurora field generator unit contains coils that generate the electromagnetic field.

Sensor coils imbedded into the tracked tool are exposed to the produced electromagnetic field and these sensors measure the induced voltage. The induced voltage is then used to calculate the position and orientation of the sensor coils. The coils return the sensor position and orientation with five (5D) or six degrees (6D) of freedom (x , y , z translations and two or three

orientations). A disadvantage of magnetic localizers is that they induce eddy currents in nearby conductive materials. These eddy currents create an opposing magnetic field to the original external magnetic field. The intersection of Aurora's magnetic field with the opposing magnetic field disrupts the magnetic field and can affect the transformation data produced. This leads to systematic tracking errors.

Several groups have studied the effect of metallic materials on the accuracy of a magnetic tracker [5-7]. From equation 1[6], the error in the reported position due to a metallic object Δr is predicted to be

$$\Delta r \propto \frac{d_{tr}^4}{d_{tm}^3 d_{mr}^3} \quad 3$$

d_{tr} is the distance between the field source (transmitter) and the sensor (receiver), d_{tm} the distance between the field source (transmitter) and the metal and d_{mr} the distance between the metal and the sensor (receiver). From equation 3, it can be observed that the error in localizing a point decreases as the metal-transmitter and metal-receiver distances are increased. This indicates that although metals in the working volume can lead to incorrect sensor readings, careful placement of the transmitter and the sensor in relation to the metals in the environment can help reduce the amount of error in the measured position of the sensor.

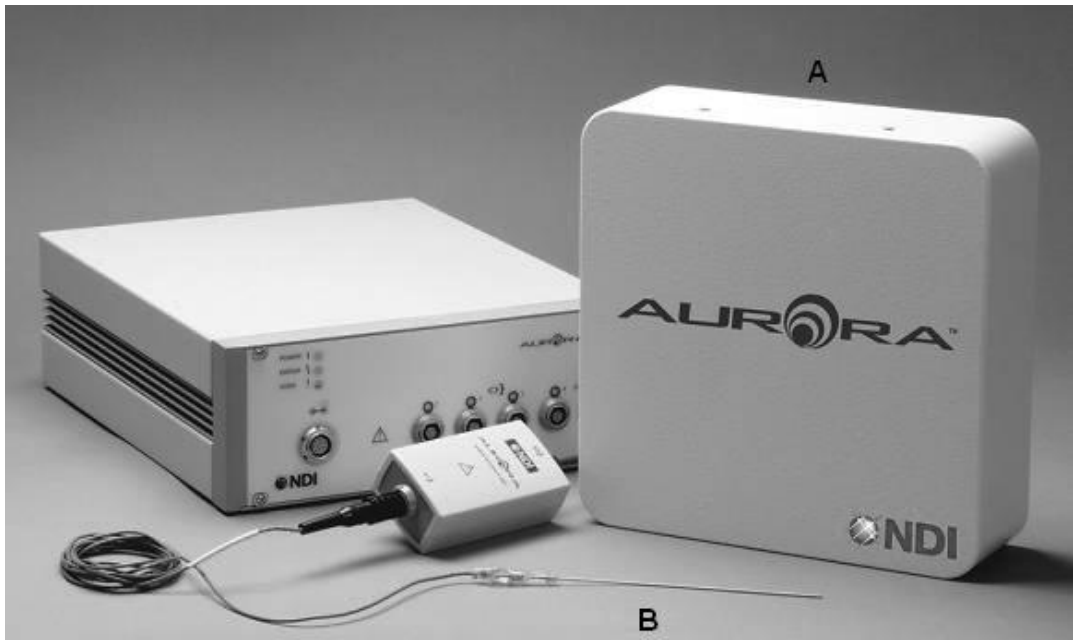


Figure 5: Diagram of the Aurora magnetic tracker. A is the field generator and B is the sensor

Before a localizer can be effectively used for image-guided procedures, characterization of the localizer is required. The fiducial localization error is a property that depends on the performance of the tracker. The expected target registration error (TRE) is a function of the fiducial localization error (FLE) and the spatial distribution of the fiducials [8]. TRE is a measure of how accurately you get to the target or area of interest. Several groups have reported a spatial and angular dependence of the root mean square (RMS) error of the magnetic tracker. This introduces a concept of non-constant FLE throughout the working volume of the magnetic tracker. The effect of angular orientation was studied by Frantz *et al.* They determined that the best orientation that produces the least error is having the sensor directed orthogonal $\pm 90^\circ$ toward the field generator and the worst orientation is when the sensor is at $(0, 180^\circ)$ toward the field generator [5].

Hummel *et al* have characterized the relative positional error of the Aurora for the 6D and the 5D sensors [4, 7] for a plane intersecting the magnetic field. They found a spatial dependence on the RMS error of the plane. A plane intersecting the magnetic field does not give all the information about the FLE needed for an image-guided procedure. The fiducials required for an image-guided procedure are normally placed on different planes intersecting the working volume of the magnetic tracker. A volumetric map of the errors in a subset of the working volume of the magnetic field that the fiducials will be placed on will help accurately predict the FLE that will be observed during the procedure. It will also help predict the TRE that will be observed at given positions from the magnetic tracker.

Volumetric calibrations have been done using a robot arm that is randomly moved through the volume of the Aurora [5]. This was done on the first-generation Aurora tracking device. The Aurora tracker that is being used for this paper is the second-generation Aurora

tracker. There has been a considerable increase in the accuracy of the system from the first-generation to the second-generation system [4]. The results were also reported as a function of the radial distance from the tracker. The radial distance calculation assumes a known center for the magnetic field source in the field generator. Since the magnetic field source position is unknown, a radial distance does not help in determining the FLE at certain distances from the surface of the Aurora tracker. Also Wilson *et al* proposed a protocol for the evaluation of the accuracy of the Aurora in a volume. This was done with a cubic phantom with holes drilled at random positions throughout the volume. They obtained the average error in the working volume of the Aurora with the field generator at different distances from the field generator and at different environments [9]. We propose to get planar errors so that errors in each plane can be evaluated separately. For purposes of image guidance, the FLE that can be expected at certain distances in the three cardinal planes from the Aurora will be useful for the placement of the Aurora magnetic tracker during the image-guided procedure. Planar results will help determine the change in errors in the system with respect to the different cardinal planes of the Aurora. This will help determine the error that will be expected at different distances from the Aurora field generator.

The purpose of this work is to perform a volumetric characterization of the FLE in the working volume of the Aurora magnetic tracker by sampling the magnetic field using a tomographic grid. Since the Aurora magnetic tracker will be used for image-guided transorbital procedures we chose a working volume that was close to the average size of the human head.

Materials and methods

To characterize the error in the magnetic tracker, a 22.6 cm by 22.6 cm square Plexiglass grid phantom with 11 by 11 divots 0.8 inch (2.032 cm) apart as shown in Figure 6 was constructed. The divots were 1 mm in radius drilled with a machine precision of 25 μm . The dimensions of the phantom (22.6 cm²) were chosen to be close to the average size of a human head. For the measurements we chose the tracker to be 7.4 cm away from the first divot. This was chosen as a minimal convenient distance the magnetic field generator could be at for the tracker to be used for image-guided transorbital guidance without the physician bumping into the tracker during the procedure. Figure 8 shows a layout of the setup used for the data collection. For our measurements we chose the sensor to be orthogonal to the field generator. The phantom was designed to limit the variation in the angles of the sensors during data collection. We acknowledge that they may be angular dependences in the measured error but that is beyond the scope of this paper. Prior to the measurements, the plate and field generator were rigidly attached to a wooden board.

FLE of the tracker

The FLE of the magnetic tracker can be modeled as sum of the random component of the FLE and the spatial component of the FLE.

$$\text{FLE}_{\text{total}} = \text{FLE}_{\text{random}} + \text{FLE}_{\text{spatial}} \quad 4$$

The random component of the FLE is a result of the localization noise in the system. It is the precision in localizing the same point using the magnetic tracking system.

$$\text{FLE}_{\text{random}} = \text{FLE}_{\text{mechanics_of_tracker}} + \text{FLE}_{\text{repositioning}} \quad 5$$

To remove the effect of the FLE due to the repositioning of the sensor during data collection, one set of continuous time points were taken for each measurement. The random FLE due to the mechanics of the tracker is the error due to the internal workings of the tracker. It measures the error such as the stability of the coils that produce the magnetic fields and the stability of the sensors and the position calculation algorithm. The random FLE due to the mechanics of the localizer was calculated as the sum of the variance of the signal in the three cardinal planes.

$$\langle FLE_{\text{random}}^2 \rangle = \sigma_x^2 + \sigma_y^2 + \sigma_z^2 \quad 6$$

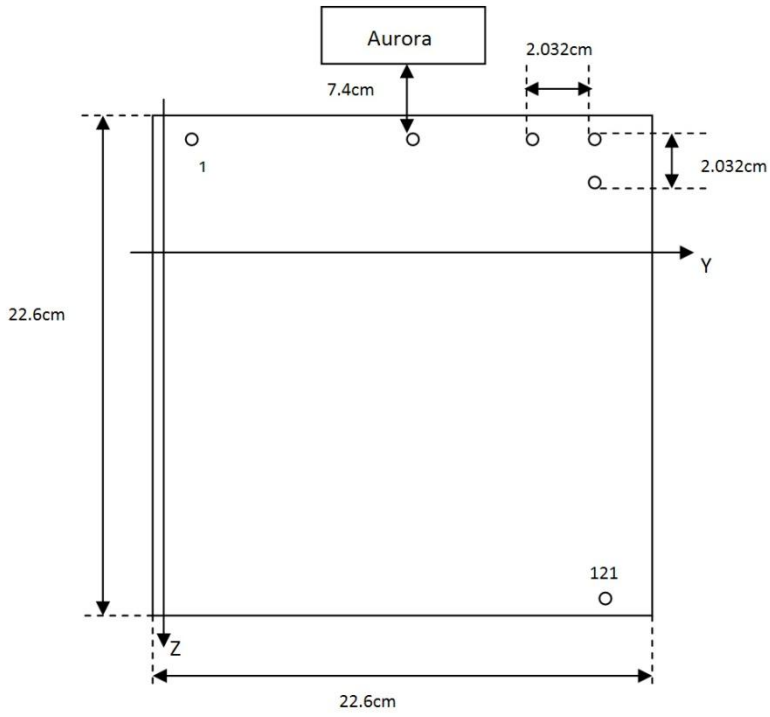
The spatial FLE is the accuracy of the localized point compared to the “true” value of the point. Since the “true point” cannot be defined, the relative spatial FLE of the magnetic tracker was calculated instead.

$$FLE_{\text{spatial}} = FLE_{\text{absolute}_{\text{aurora_divot}}} + FLE_{\text{relative_spatial}} \quad 7$$

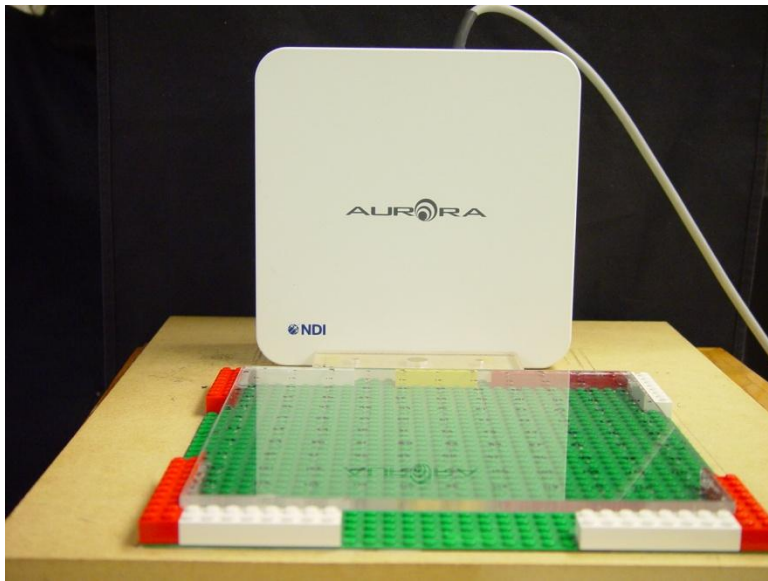
The relative spatial component of the FLE was calculated using the grid experimental setup in figure 2. The absolute distance between the first rows of divots closest to the tracker is subtracted from all the subsequent grid rows and this is compared to the actual machine precision distance of the divots. This is done for the 3 cardinal plane positions to give a spatial error distance map of the plane intersecting the magnetic tracker at sampled points.

$$FLE_{\text{relative_spatial}} = |Dist_{\text{aurora}} - Dist_{\text{machine}}| \quad 8$$

$Dist_{\text{aurora}}$ is the distance between the rows of divots in Aurora space and $Dist_{\text{machine}}$ is the machine precision distance.



A



B

Figure 6: Schematic and setup of the grid used for the measurement. A shows grid measurements and B shows the setup for the data collection.

To determine the number of data points to be collected for the FLE measurements, 1000 continuous points were collected for two divots (1 and 121). These divots corresponded to the beginning of the grid and the last point of the grid. Different continuous time samples were used to calculate the variance of the data in order to determine the change in the variance of the data as a function of the number of sampled points used for the calculation. The first 50 points were initially selected and this was increased incrementally by 50 points to 1000 points. Figure 7 shows the graph of the variance calculated with different number of time measurements. Table 2 also shows the maximum and minimum variance obtained using the different time points and the variance obtained using 150 points. From Figure 7 and Table 2 , it can be observed that deviations in the variance from the variance calculated with 150 points were not significant when compared to the minimum variances measured between 50 and 1000 points. Therefore 150 points can accurately predict the variance of the time points and thus predict the FLE of the system. So for the calculation of both the random and the relative spatial error of the magnetic tracker, 150 points were used.

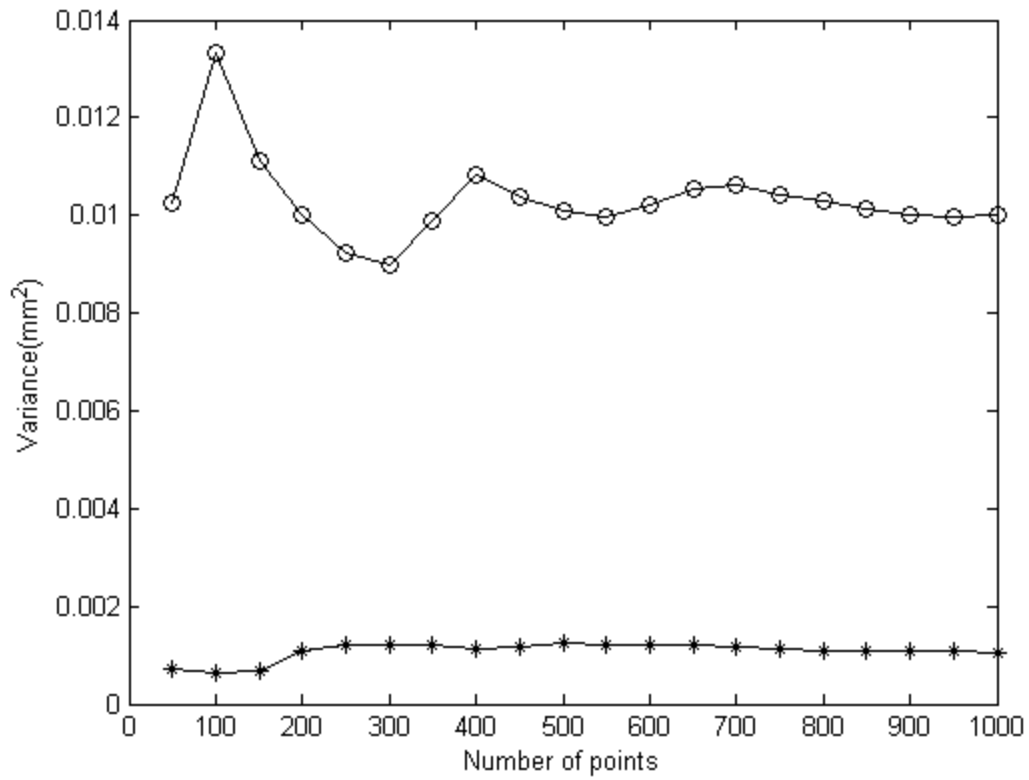


Figure 7: Variance calculated for fiducial 1 and 121 using 50 to 1000 points. The asterisks represent fiducial 1 and circles represent fiducial 121.

Table 2: The minimum and the maximum variances obtained for fiducials 1 and 121 and the number of points that correspond to the minimum and maximum values. Table also shows the variance calculated with 150 points.

Fiducial Number	Min(mm ²) (Points producing minimum)	Max(mm ²) (Points producing maximum)	Error for 150 points(mm ²)
1	0.0006 (100)	0.0012 (500)	0.0007
121	0.0090 (300)	0.0133 (100)	0.0111

A volumetric map of the magnetic space forming a type of tomographic phantom was performed by moving the flat Plexiglass phantom up in the x -axis in increments of 38.4 mm from 9.6 mm to 201.6 mm. The final stopping distance was chosen to correspond to the average size of the human head. Figure 8 shows a schematic of the movement of the planes. For each plane, a 5D and a 6D sensor were used to localize each divot and the random and the relative spatial FLE of each plane was calculated. The sensors used in each case were a 6D probe and a 5D flexible catheter that were manufactured by Northern Digital Inc, Waterloo, Ontario.

Figure 9 is a schematic of the measurements of the orbit and the different possible positions of the field generator for the image-guided transorbital procedure. Since the target of our endoscopic guidance is the orbital space behind the optic nerve, the maximum distance between the field generator and the sensor can be calculated depending on the placement of the field generator from the skull.

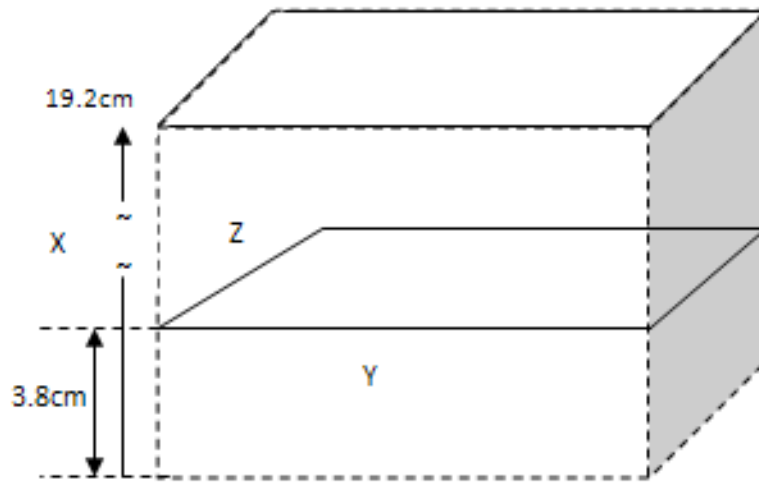


Figure 8: Schematic of the volumetric movement of the measurement grid for the endoscopic procedure.

As shown in Figure 9, positions A, B and C give some of the possible positions of the field generator for the image-guided procedure. Ideally, position C will reduce the chances of the tracker being bumped by the physician during the procedure.

Figure 10 shows a schematic of the orbital measurements in position A. From Figure 10, if $c = 4$ cm, $0 < b \leq 5$ cm then $a < 4$ cm. Therefore the maximum z distance expected for position A is 4 cm. For position B, the maximum z distance expected is 5 cm and for position C, the maximum z distance expected is 10.5 cm. These distances were used to calculate the average error that can be expected from the magnetic tracker if the field generator was kept at those positions during the image-guided procedure. This was done by calculating the average error from $0 < z < \text{maximum } z$. $z = 0$ corresponds to the starting point of the measurement with the tracker 7.4 cm away from the sensor. Because of the setup of the grid, the nearest values that were equal to or more than the calculated z values for positions A to C were chosen. We choose $A = 4$ cm, $B = 6$ cm and $C = 12$ cm.

Effect of an endoscope on the accuracy of the magnetic tracker

Since the transorbital procedure is envisioned as an outpatient procedure that can be performed in a procedure room, the metals in the environment can be accounted for. To find out the effect of an endoscope on the flexible magnetic sensor, points were collected for a divot at a z value of 6 cm. The divot was localized with only the 5D probe for a baseline measurement and also localized with the sensor touching a flexible endoscope (Storz Flex X2, Karl Storz Endoscopy America Inc). This was done ten different times and for each time the probe was removed and the point was localized again. The mean of the 1500 points for the two different measurements was calculated and this was used to calculate the effect of the endoscope on the flexible 5D sensor.

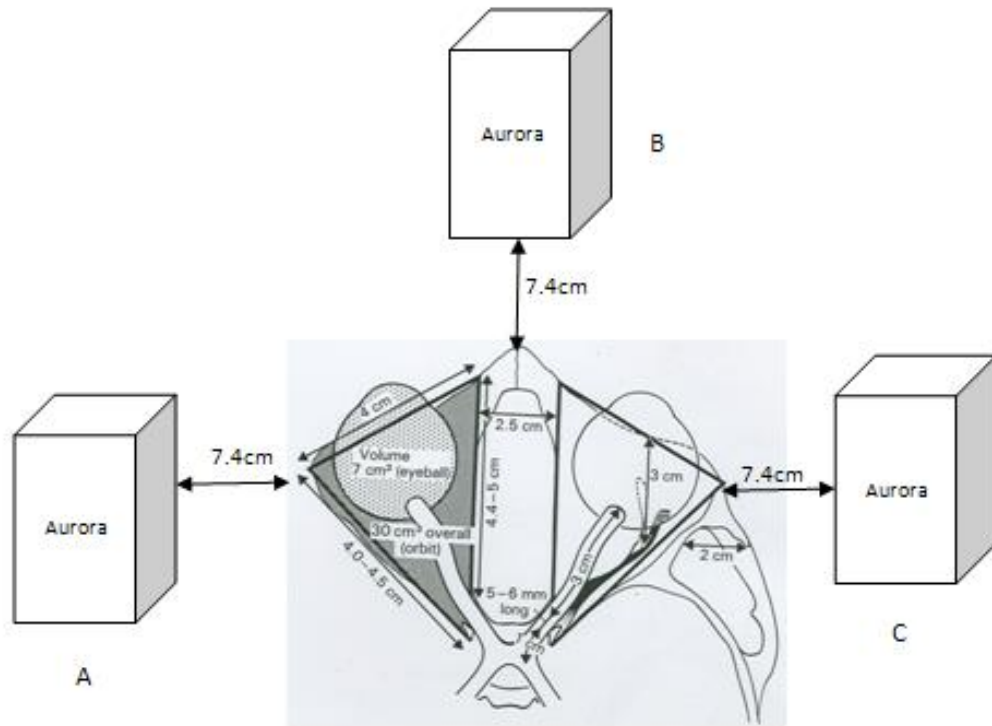


Figure 9: Schematic of the different possible positions of the Aurora system. The dark gray orbital region shows the orbit of interest

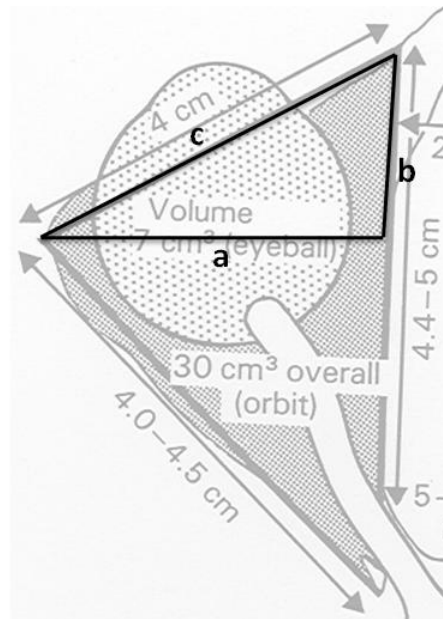


Figure 10: The schematic of the orbital triangle formed for position A in Figure 9.

Results

As expected the error increases in the z direction as the distance between the magnetic sensor and the field generator increases. This increase was found in both the random FLE and the relative spatial FLE of the tracker. Figure 11 shows a sample plane of the random FLE of both the 5D and the 6D sensors. From the graph, it can be observed that the random FLE of the 5D sensors fluctuates more than the random FLE of the 6D sensors.

The magnitude of the random error observed for the 6D sensor is smaller than that of the 5D sensor for each grid position and across the planes. The difference in the range of errors observed can be attributed to the manufacture of the sensors. The 6D sensors have a redundancy in them because they are made up of two 5D sensors that are at right angles to each other. This reduces the error observed while using the 6D sensors. The average random error observed across all the six planes and all the grid points for the 6D sensor is 0.093 ± 0.064 mm and the average random error observed for the 5D sensor is 0.193 ± 0.10 mm.

The spatial error also increases as a function of the distance of the sensor from the field generator. Figure 12 shows a sample plane of the relative spatial error of both the 5D and the 6D sensors. On average, the relative spatial error for the 6D tracker is smaller than the relative spatial error for the 5D tracker for all the grid points and across all the planes. The average relative spatial FLE across the six planes and all the grid points for the 6D sensor was 1.35 ± 1.16 mm and the average relative spatial FLE for the 5D sensor was 2.34 ± 1.76 mm.

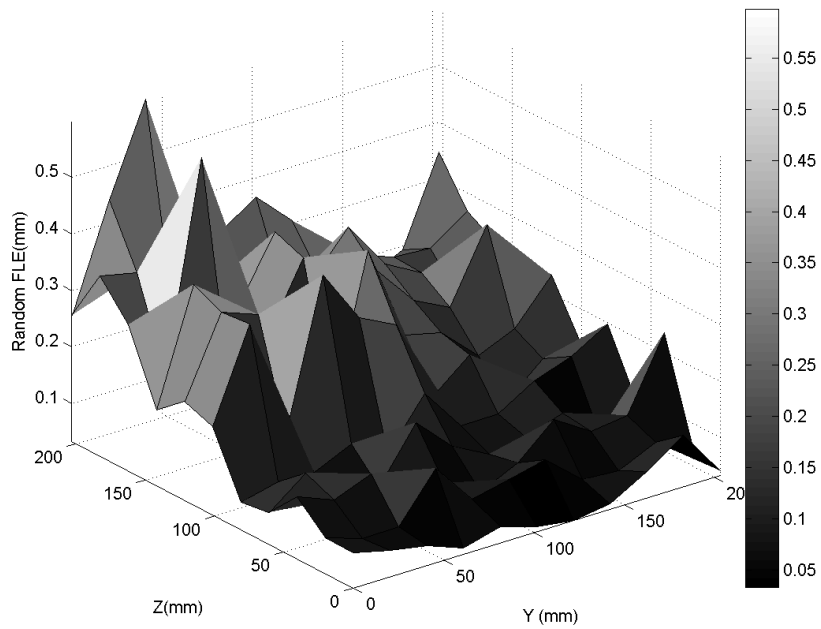
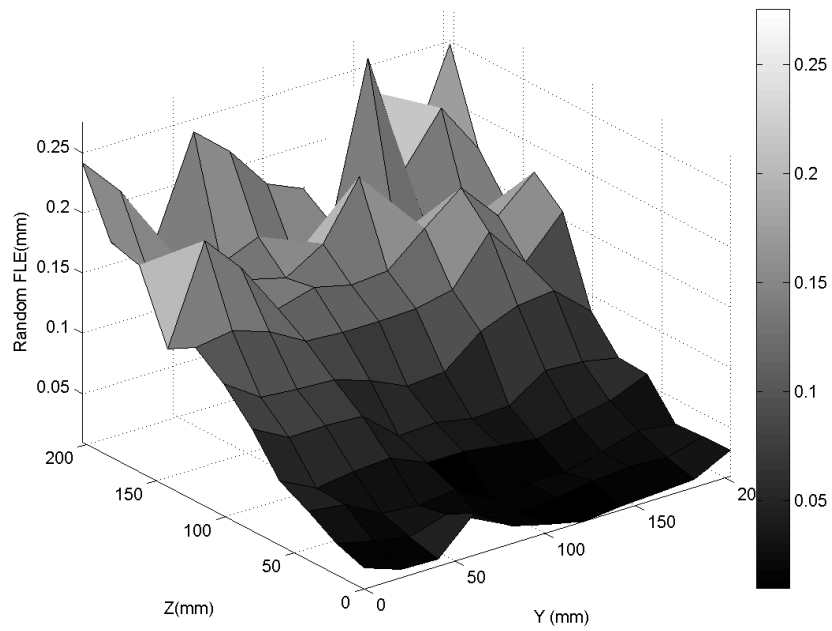


Figure 11: Graph of the random FLE of a sample plane (plane 2) intersecting the magnetic field. Figure on the left is the 6D and the figure on the right is the 5D.

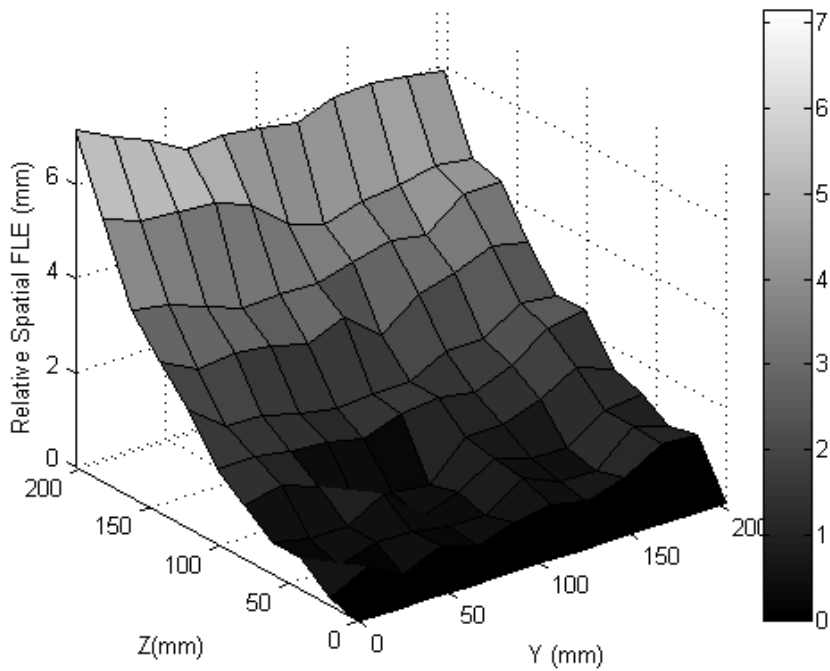
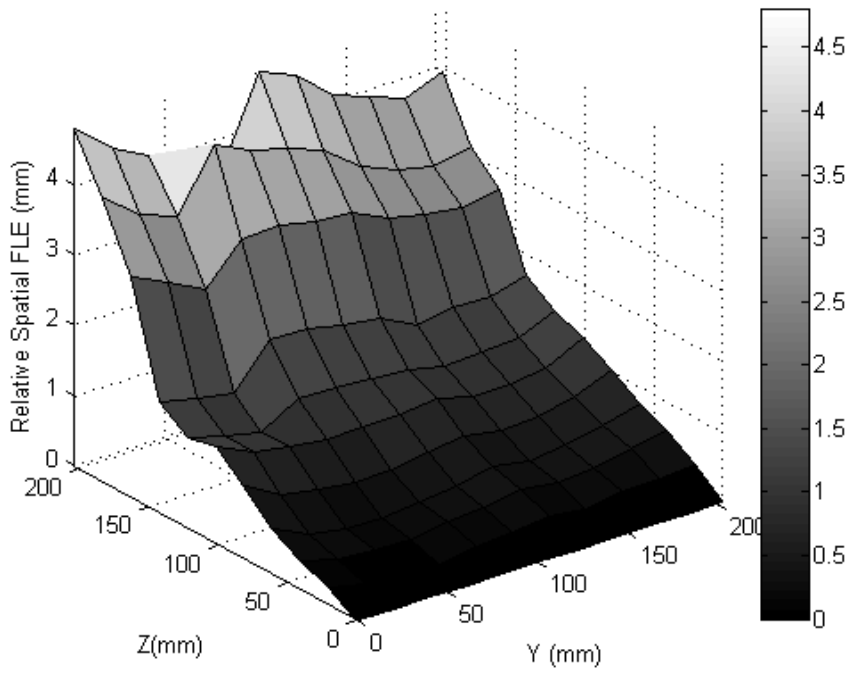


Figure 12: Figure showing the relative spatial error of a sample plane (plane 5) intersecting the magnetic field. The figure on the left shows the error for the 6D and the figure on the right shows the error for the 5D tracker.

The random FLE and the relative spatial FLE for the different field generator positions in Figure 9 was calculated.

Tables 3 and 4 show the statistical values obtained for the random FLE and the relative spatial FLE for the $z = 4$ cm (position A) for both the 5D and the 6D sensors. The magnitude of the random and the relative spatial FLE for the 6D tracker is smaller than the magnitude of the random and the relative spatial FLE for the 5D tracker for all the planes for position A. There is a slight decrease in the average random and relative spatial FLE from plane 1 to plane 2 for both the 5D and the 6D sensors. The errors increase from plane 2 to 3, which leads to a possibility of a minimum occurring between plane 2 and plane 3 for the relative spatial FLE of both the 5D and the 6D sensors. The average random and relative spatial FLE was calculated across all the six planes. The average random FLE in all the six planes is 0.029 ± 0.014 mm for the 6D probe and 0.125 ± 0.063 mm for the 5D probe. The mean relative spatial FLE in all the six planes is 0.33 ± 0.22 mm for the 6D probe and 0.78 ± 0.37 mm for the 5D sensor.

Tables 5 and 6 show the statistical values obtained for $z = 6$ cm. The average random FLE in all the six planes is 0.034 ± 0.017 mm for the 6D probe and 0.127 ± 0.063 mm for the 5D probe. The same dip in the error described for $z = 4$ cm was observed for the FLE of the system at $z = 6$ cm. The average spatial FLE for the six planes is 0.40 ± 0.27 mm for the 6D probe and 0.86 ± 0.42 mm for the 5D probe.

Table 3: Random FLE of both the 5D and the 6D sensors for a z value of 4cm

Planes	Random FLE (mm) (6D)				Random FLE (mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.026	0.011	0.011	0.055	0.144	0.062	0.034	0.260
2	0.025	0.010	0.010	0.050	0.089	0.042	0.033	0.234
3	0.024	0.014	0.008	0.066	0.107	0.044	0.043	0.217
4	0.025	0.015	0.007	0.070	0.163	0.088	0.070	0.380
5	0.028	0.011	0.013	0.054	0.108	0.053	0.041	0.264
6	0.045	0.014	0.025	0.087	0.141	0.043	0.079	0.240

Table 4: Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 4cm

Planes	Relative Spatial FLE(mm) (6D)				Relative Spatial FLE(mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.40	0.17	0.15	0.76	0.78	0.46	0.20	1.85
2	0.19	0.08	0.05	0.39	0.72	0.21	0.31	1.19
3	0.23	0.19	0.03	0.85	0.80	0.28	0.16	1.19
4	0.22	0.11	0.07	0.49	0.81	0.36	0.26	1.73
5	0.28	0.13	0.06	0.59	0.60	0.31	0.16	1.23
6	0.63	0.25	0.28	1.11	0.98	0.47	0.22	2.06

Table 5: Random FLE of both the 5D and the 6D sensors for a z value of 6cm

Planes	Random FLE (mm) (6D)				Random FLE (mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.031	0.015	0.011	0.091	0.158	0.066	0.034	0.303
2	0.030	0.014	0.010	0.063	0.091	0.040	0.033	0.234
3	0.029	0.016	0.008	0.073	0.102	0.042	0.043	0.217
4	0.028	0.016	0.007	0.070	0.150	0.081	0.069	0.380
5	0.034	0.017	0.013	0.107	0.113	0.051	0.041	0.264
6	0.050	0.015	0.025	0.087	0.148	0.052	0.079	0.276

Table 6: Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 6cm

Planes	Relative Spatial FLE(mm) (6D)				Relative Spatial FLE(mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.48	0.20	0.15	0.89	0.80	0.48	0.20	2.20
2	0.25	0.13	0.05	0.52	0.74	0.30	0.20	1.56
3	0.28	0.22	0.03	1.00	0.90	0.37	0.16	1.89
4	0.29	0.16	0.07	0.77	0.94	0.38	0.26	1.73
5	0.35	0.16	0.06	0.73	0.66	0.32	0.16	1.33
6	0.77	0.31	0.28	1.40	1.10	0.52	0.22	2.36

Table 7: Random FLE of both the 5D and the 6D sensors for a z value of 12cm

Planes	Random FLE (mm) (6D)				Random FLE (mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.048	0.026	0.011	0.115	0.195	0.101	0.034	0.568
2	0.058	0.040	0.010	0.158	0.131	0.081	0.033	0.397
3	0.049	0.031	0.008	0.145	0.126	0.057	0.040	0.288
4	0.048	0.030	0.007	0.136	0.171	0.078	0.069	0.380
5	0.057	0.038	0.013	0.198	0.127	0.048	0.041	0.264
6	0.077	0.047	0.025	0.235	0.160	0.064	0.079	0.445

Table 8: Relative Spatial FLE of both the 5D and the 6D sensors for a z value of 12cm

Planes	Relative Spatial FLE(mm) (6D)				Relative Spatial FLE(mm) (5D)			
	Mean	Standard deviation	Minimum	Maximum	Mean	Standard deviation	Minimum	Maximum
1	0.61	0.23	0.15	1.24	1.02	0.53	0.20	2.76
2	0.40	0.25	0.05	1.20	0.86	0.38	0.16	1.65
3	0.50	0.36	0.03	1.71	1.32	0.67	0.16	3.36
4	0.56	0.38	0.07	1.77	1.42	0.69	0.26	3.29
5	0.68	0.39	0.06	1.41	1.12	0.65	0.16	2.53
6	1.17	0.53	0.28	2.22	1.62	0.76	0.22	3.56

Tables 7 and 8 show the statistical observation for each plane at $z = 12$ cm. The mean random FLE for the 6D probe is 0.056 ± 0.037 mm and 0.152 ± 0.078 mm for the 5D probe. The relative spatial FLE was $0.65 \pm .44$ mm for the 6D and 1.23 ± 0.67 mm for the 5D probe. The dip in error observed for $z = 4$ and $z = 6$ cm was also observed in $z = 12$ cm.

Effect of the endoscope on the 5D sensor

The variance and the RMS error of the means of the 1500 points collected for the divot with and without the endoscope were calculated. The variance of the divots without the endoscope was 0.076 mm² and the variance of the divot points with the endoscope was 0.081 mm². This corresponds to a 0.0089 mm increase in the FLE of the sensor–endoscope configuration versus the FLE of only the 5D sensor. The RMS error between the means of the two divot points was 0.2 mm.

Discussion

In this paper, we characterized the fiducial localization error and the relative spatial errors of a subset of the working volume of the Aurora tracker. This subset corresponds to the average size of the human head. We observed that there was an increase in both the relative spatial FLE and the random FLE of the tracker as the sensor moved further away from the tracker in the z direction. We also observed that there was a dip in both the random and the relative spatial FLE of the tracker as we sampled planar intersection of the working volume of the tracker. There was a decrease in relative spatial error from plane 1 to 2. After plane 3 the error starts increasing from the error in plane 2. Since the slice steps are fixed, the minimum values in the slice direction are never observed. By interpolation of tables 4, 6 and 8 the most likely place for the minimum seems to be between slices 2 (48 mm from the base of the Aurora) and 3 (86.4 mm from the base

of the Aurora). We also observed that the major component of the FLE of the magnetic tracker is the spatial FLE.

Since the 6D probe is more accurate than the 5D probe, the 6D probe will be used for the rigid registration process to transform the Aurora tracker space into the image space and then the 5D probe will be used for the guidance. Although the 6D probe is more accurate than the 5D probe, at this time, the sensors that can be embedded into the endoscope for transorbital image guidance are the 5D sensors.

The error characterization was made to be as realistic as possible because the localization process was done by hand to mimic what will be observed in an image-guided procedure done with the magnetic tracker. This gives an error that may be slightly larger than the absolute error of the Aurora tracker. Also the relative spatial FLE was calculated instead of the absolute spatial FLE because the origin of the Aurora system is unknown. The spatial error can be calculated from the relative spatial error by adding the absolute error from the first row of divots to the field generator to the relative spatial error. Even though the error observed may not be equal to the absolute error of the system, the error characteristics of the tracker will follow the trend observed with the error increasing as the distance between the field generator and the sensor increased and also the minimal error of the tracker being above the base of the tracker.

The procedure that the magnetically tracked endoscope will be used for will be a minimally invasive drug delivery procedure that will be carried out in a procedure room. Since the procedure will be done in a doctor's procedure room instead of an operating room, the metals in the environment can be controlled and as such will not affect the accuracy of the magnetic tracker. The flexible endoscope that will be used for the procedure was shown not to have a significant effect on the accuracy of the 5D flexible probe. There was a 0.2 mm increase in the

RMS error between the sensor and the sensor–endoscope configuration. The error observed incorporates both the repositioning error and the error due to the effect of the flexible endoscope. Therefore the error due to the endoscope may be less than 0.2 mm.

One of the advantages of transorbital endoscopic procedures is the fact that the orbit is a small space and FLE of the tracker do not degrade as much in the working volume required for the procedure. This was evidenced in the calculations of the FLE for the different field generator positions shown in Figure 9. For the different field generator placements we found an average random FLE to be less than 0.06 mm for the 6D probe and 0.2 mm for the 5D probe. We also observed an average relative spatial FLE of less than 0.7 mm for the 6D probe, 1.3 mm for the 5D probe. We plan on incorporating these findings in the placement of the Aurora field generator during the image-guided transorbital procedure.

References

1. Zhang, H., et al., *Electromagnetic tracking for abdominal interventions in computer aided surgery*. Computer Aided Surgery, 2006. **11**(3): p. 127-136.
2. Wood, B.J., et al., *Navigation with Electromagnetic Tracking for Interventional Radiology Procedures: A Feasibility Study*. Journal of Vascular and Interventional Radiology, 2005. **16**: p. 493-505.
3. Krucker, J., et al., *Electromagnetic tracking for thermal ablation and biopsy guidance: clinical evaluation of spatial accuracy*. Journal of Vascular & Interventional Radiology, 2007. **18**(9): p. 1141-50.
4. Hummel, J.B., et al., *Evaluation of a new electromagnetic tracking system using a standardized assessment protocol*. Physics in Medicine and Biology, 2006. **51**: p. N205-N210.
5. Frantz, D.D., et al., *Accuracy assessment protocols for electromagnetic tracking systems*. Physics in Medicine and Biology, 2003. **48**(14): p. 2241.

6. Mark A. Nixon, B.C.M., W. Richard Fright and N. Brent Price, *The Effect of Metals and Interfering Fields on Electromagnetic Trackers*. Presence, MIT Press, 1998. **7**(2): p. 204-218.
7. Hummel, J.B., et al., *Design and application of an assessment protocol for electromagnetic tracking systems*. Medical Physics, 2005. **32**(7): p. 2371-2379.
8. Fitzpatrick, J.M., J.B. West, and C.R. Maurer, Jr., *Predicting error in rigid-body point-based registration*. Medical Imaging, IEEE Transactions on, 1998. **17**(5): p. 694.
9. Wilson, E., et al., *A hardware and software protocol for the evaluation of electromagnetic tracker accuracy in the clinical environment: a multi-center study*. Medical Imaging 2007: Visualization and Image-Guided Procedures: Proc. of SPIE, 2007. **6509**: p. 65092T-1-11.

CHAPTER IV

MANUSCRIPT 2- Sensitivity analysis of fiducial placement on transorbital target registration error.

Atuegwu N C and Galloway R L

Original form of manuscript appears in IJCARS Volume 2, Number 6 April, 2008, pages 397-

404

Abstract

Objective In many clinical applications of image-guided surgery, skin fiducial placement is poorly defined and occasionally poorly executed, leading to an increase in the target registration error (TRE). Fiducial placement analysis usually focuses on a single target, where surgical guidance requires accurate localization of a region or volume of tissue. To address these limitations, a method of fiducial positioning for minimizing the TRE in a target region was developed.

Method This methodology uses patient specific anatomic data, the patient skin surface and accounts for areas which may be poor choices for fiducial placement due to likely fiducial motion. The effect of skin motion on the expected TRE of a target region was modeled and evaluated. Transorbital therapy delivery was selected as the application of interest, so facial morphology is of greatest importance. Our target region is the pyramidal space behind the globe of the eye. A laser range scan of the face of a skull phantom with taboo regions chosen semiautomatically was used as an input to the simulated annealing optimization algorithm.

Results Optimizing the fiducial position reduced the expected TRE by 50% when compared to an unoptimized fiducial placement. In addition, the effect of fiducial motion or localizer fiducial localization error is also reduced in the optimized version.

Conclusion Improved registration results for transorbital therapy delivery were achieved semiautomatically using optical facial surface scans for image-guided surgical localization. The target registration error minimization method was feasible for in vivo applications.

Introduction

Image guided surgery (IGS) requires a registration between an object in physical space and the same object in image space. The most common method of registration used for IGS is point based registration. The most effective point based registration uses extrinsic objects that are attached to patients such extrinsic objects or anatomic landmarks are referred to as fiducial markers.

The quality of fiducial-based registration may be judged by several types of registration error computed after the registration. The three main measures of registration are fiducial localization error (FLE), fiducial registration error (FRE) and target registration error (TRE). FLE is the error in locating the position of a fiducial in any space. FRE is the distance between corresponding fiducial points after registration. TRE is the distance between the corresponding “target” points after registration. “Target” in this case means points other than the fiducial points [1]. FLE is affected human error in the placement of the tracking probe during localization of the fiducials and the error associated with the tracking system [2].

Two basic types of fiducial markers are used in neurosurgical IGS: bone implantable markers [3] and skin surface fiducials [4]. Bone implanted fiducials generally are more invasive and cannot be used for procedures that are repetitively done on a patient. Skin fiducials are not invasive and can be used frequently on a patient. Since skin moves over the bone, skin fiducials are by nature, more mobile than bone implantable markers, and this may lead to an increase in

the localization error of the skin fiducials. This increase in localization error leads to an increase in TRE during the IGS procedure.

Fiducial registration theory is based on localization of the fiducial points and several presumptions. These presumptions are that extrinsic objects that define the fiducial points do not move relative to the anatomy of the patient and other markers, the surgical target is a constant point and that all positions for markers have equal likelihood or utility.

The paper deals with the fact that the target is rarely a point but a region. It also deals with motion of skin fiducials relative to both the anatomy of the patient and to other fiducials. It also deals with the fact that there are positions where the fiducials cannot be applied on the patient and that all positions of markers do not have equal utility. The places where the fiducials cannot be applied to are referred to as the “taboo” regions. Also the fiducials have physical constraints such as the size and the shape of the fiducial that further affect the placement of the fiducials.

Optimizing the fiducial arrangement can decrease the TRE obtained after registration. This is especially important when the target is a target zone as opposed to a target point and when the FLE of the system is high; as in the case of a magnetic tracker, which has shown FLE values of about 1-10mm in parts of the work volume [5, 6]. Also skin motion can lead to a further increase in FLE during registration. Optimal placement of the skin fiducials in less mobile parts of the skin and the avoidance of areas that may be deformed or shifted during the imaging and surgical procedure can lead to a reduction in the overall FLE associated with skin fiducials [1].

Several groups have shown that the arrangement of fiducials before point based registration affects TRE obtained after registration[1, 7, 8] West et al proposed some guidelines

for fiducial placement given a certain target[1]. Liu et al showed an improvement in TRE by optimizing random skin fiducial positions used during photogrammetry based patient positioning systems. In both cases, the groups did not take into account patient specific geometry, the areas that the fiducials cannot be placed on due to obstruction of the surgeons view and also areas that are more likely to move when skin fiducials are placed.

The purpose of this paper is to present a semiautomatic method of fiducial positioning for minimizing the TRE in a target region subject to the surgical space available and parts of the surface that are less liable to skin motion. This removes the guesswork in image placement for a particular patient. The paper also explores the effect of skin motion or fiducial localization errors on TRE in a target zone. Our laboratory has been working on image guided endoscopic drug delivery to the optic nerve therefore the paper will specifically explore the minimization of the TRE in the region occupied by the optic nerve eye junction. In the case of image guided endoscopic drug delivery, the procedure will be done multiple times a year and as such requires skin fiducials. Also a magnetic tracker will be used for the endoscopic guidance. Since the FLE associated with a magnetic tracker is high, an optimization of fiducial placement is essential.

Materials and Methods

TRE analysis

Equation 9 shows the relationship between TRE, FLE and the number and position of fiducials used for the registration [7]

$$\langle TRE^2 \rangle = \langle FLE^2 \rangle \left(\frac{1}{N} + \frac{1}{K} \sum_{i=1}^K \sum_{j \neq i}^K \frac{r_i^2}{\Lambda_{ii}^2 + \Lambda_{jj}^2} \right) \quad 2$$

N = Number of fiducials

K = Spatial dimension; $K=3$

r_i = Distance between the centroid of the fiducials and the target

Λ =Eigenvalues of the fiducial arrangement

To minimize the TRE at a target point, equation 9 above has to be minimized. From equation 9, the number of fiducials and the FLE can be assumed to be constant; therefore the minimization of the rotational component of the TRE minimizes expected TRE.

Therefore,

$$\min \langle TRE^2 \ r \rangle = \min \left(\frac{1}{K} \sum_{i=1}^K \sum_{j \neq i}^K \frac{r_i^2}{\Lambda_{ii}^2 + \Lambda_{jj}^2} \right) = R \ r \quad 3$$

To minimize the objective function R(r), simulated annealing (SA) was used. SA employs a random search which not only accepts changes that decrease the objective function but also some changes that increase it. SA's major advantage over other methods is an ability to avoid becoming trapped in local minima. The disadvantage of SA is that it can be computational expensive as the algorithm can keep “bouncing around” as probabilities that can increase the objective function can be chosen. An optimized simulated annealing method from Bohachevsky et al[9] was used. This reduced the computational time by introducing variables that controlled the acceptance of probabilities as the solution neared the global optimum. Also since SA involves a probabilistic method, a slightly different answer can be obtained for the same optimization function.

SA Algorithm pseudocode

1. Initial positions for all the fiducials are chosen. $X_0 = x_1, x_2, x_3, \dots, x_N$; N is the number of fiducials used. The initial positions are chosen to be in the regions other than the avoid regions. This is the input to the algorithm.
2. $\phi \ x$ is the function to be minimized; ϕ_m is the value at the minimum
3. Find the nearest d_r neighbors to X_0 . d_r is the region that the SA algorithm search can move to for the next search.

4. $\phi_0 = \phi_{X_0}$. If $|\phi_0 - \phi_m| < \varepsilon$ stop
5. Random direction. Get a random neighbor from d_r points and use that as the new direction. Generate new values X_1 .
6. If any component of X_1 is in the taboo or no overlap zone. Go back to 5. Otherwise set $\phi_1 = \phi_{X_1}$ and $\Delta\phi = \phi_1 - \phi_0$. Do this for a fixed number N_d and then choose a new random point from the surface if X_1 is still in taboo region.
7. $\phi_1 \leq \phi_0$, set $X_0 = X_1$ and $\phi_0 = \phi_1$. If $|\phi_0 - \phi_m| < \varepsilon$ stop otherwise go the step 3.
8. If $\phi_1 > \phi_0$, set $p = \exp -\beta\phi_0^g \Delta\phi$. (a) Generate a uniform 0-1 random number V. (b) If $V \geq p$ go to step 5. (c) If $V < p$ set $X_0 = X_1$ and $\phi_0 = \phi_1$; and go to step 3.
9. Do 1-8 above until the maximum number of iterations is reached.

The variable β is a positive number that is chosen so that p is between 0.5 and 0.7. This prevents very few or all the searches from being accepted and g is an arbitrary negative number that makes the probability of accepting a detrimental step tend to zero as you approach the global extremum.

The algorithm minimizes the objective function until an acceptable tolerance value is reached or the algorithm reaches the maximum number of iterations and the minimal rotational error obtained during the search is used. Since the minimum rotational error that can be obtained is zero, the tolerance value was chosen to be close to zero. A value of 1e-3 was chosen as the tolerance value because from equation 9, $\frac{1}{N}$ for the procedure is at least one magnitude less than 1e-2 and therefore adding a value of less than 1e-3 to the $\frac{1}{N}$ term is not significant.

Target for the optimization

Our laboratory has been working on developing a system for drug delivery to the optic nerve. In the case of transorbital drug delivery, the main target is the optic nerve eye junction. Therefore the potential error in delivering a drug to the optic nerve eye junction needs to be determined.

Since the optic nerve moves with eye motion, the optic nerve junction cannot be assumed to be stationary and thus the TRE calculations for a stationary target cannot accurately describe the TRE that will be expected after registration in the optic nerve eye junction. To incorporate the optic nerve eye junction in the optimization scheme the path of the optic nerve junction has to be characterized. This was done by using the average maximum ocular duction of the eye and the motion of the optic nerve in mm for each degree movement of the eye.

The mean of the maximum ocular duction between age groups of 14-95 was shown to be 54° for abduction, 44 ° for adduction, 46 ° for supraduction and 51 ° for infraduction [10] Abduction is the outward movement of the eyeball, adduction is the inward movement of the eyeball, supraduction is the elevation of the eyeball and infraduction is the depression of the eyeball.

Magnetic resonance imaging-dynamic color mapping was used by Abramoff et al to calculate the motion of the optic of some healthy adult volunteers and they found that on the average the optic nerve moved an average of 0.16mm per degree[11] The optic nerve motion can then be calculated by multiplying the average optic nerve motion by the mean of the maximum ocular duction. This is shown in equation 11 below.

$$Radius(r)_{(ab,ad,su,in)} = mean_ocular_duction_{(ab,ad,su,in)} * motion_optic_nerve$$

ab = abduction

ad = adduction

su = supraduction

in = infraduction

4

This gives the maximum path transversed by the optic nerve junction during gaze. This maximum path will then be used for further TRE optimization calculations.

The orbit is roughly a quadrilateral pyramid with rounded angles, resembling a pear [12]. The space occupied by the eyeball optic nerve junction can be modeled as a cross section of the “pear shaped” orbit at a distance from the base or opening of the orbit. This can be approximated to a circle because the eyeball does not translate forwards but just moves side to side.

The radius of the circle can be approximated to be 7.5mm. This was calculated using equation 11 above. This gives the target region for the optic nerve eye junction. The target is chosen as a region that is 24mm from the surface of the eyeball. This corresponds to the average size of the human eyeball [13]. Figure 13 shows a cartoon of the target region.

For the fiducial optimization, the target zone is discretized by randomly selecting 300 points in the target zone. This was done to simulate the different possible positions of the optic nerve eye junction in the target zone. The average rotational error in the region is the evaluation of the objective function in equation 10.

Surface Acquisition

To optimize the fiducial placement, the surface of the face of a skull phantom was obtained using a laser range scan. A laser range scanner acquires three dimensional geometry of an object by scanning a laser across an object. A calibrated geometry exists between the plane of laser light and the camera. By triangulating between the observed laser image and the known

laser plane, a three dimensional point cloud representing the surface of the object is recovered. The point cloud obtained is then used as an input into the optimization algorithm

Fiducial Avoid regions

In reality, there are areas of the face on which fiducial cannot be placed on such as the eyelids. The regions are known as the “taboo regions”. A semi automatic method is used to choose these regions. Taboo regions can also be chosen to encompass other regions that the surgeon needs unobstructed during the interventions, regions that are more likely to be subject to skin motion or some patient specific regions. For the simulation, the eyelids and other parts of the face where a skin marker cannot be comfortably put on like tip of the nose and areas of the skin that were prone to skin motion was chosen as the taboo region.

Additionally since the fiducials have a finite size, a region around each fiducial that corresponds to the size of skin markers (20mm) called the “no overlap region” was automatically chosen during the calculations to avoid fiducial overlap. The “no overlap regions” simulates the condition found in real skin marker positioning.

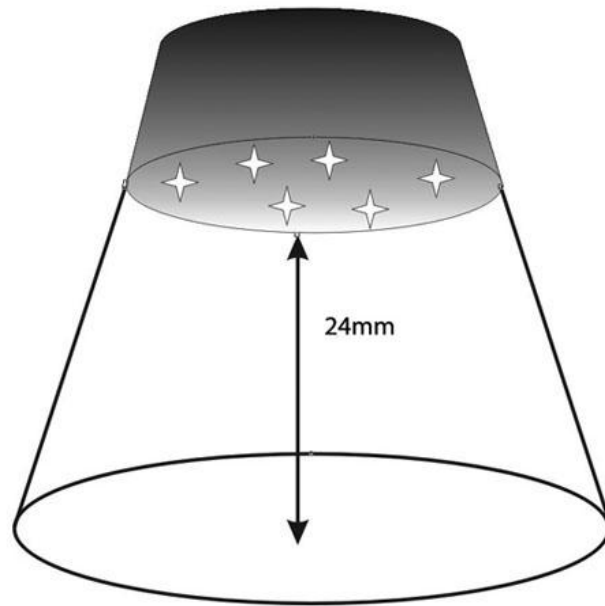


Figure 13: Cartoon of the target region. The *stars* show the target region and some of the possible locations of the target.

Determining an Optimal Fiducial Placement

To optimize the fiducial placement, the surface point cloud of the face obtained from the laser range scanner was used as an input for the optimization algorithm. Initial random fiducial positions were chosen automatically on the surface in regions other than the taboo regions and these were used as the input to the simulated annealing program. This simulates the case of the surgeons putting the fiducials on the face without any thought to the target. Because the initial fiducials are chosen not to be in the taboo region, skin motion for the initial placement is minimized. While this is clearly a worst case scenario, Labadie et al reported that users often pay little attention to the discipline required for good registration[2]. Also the fiducials are prevented from overlapping during the initial placement. The fiducials are then “moved” across the surface of the face using simulated annealing and the final optimal configuration of fiducials are determined. During the optimization, the fiducials are prevented from being located in the taboo region and also the fiducials were prevented from overlapping with each other. Also since the simulated annealing is a probabilistic method, the optimization scheme is run ten times and TRE for each run is calculated.

Skin motion Calculation

Skin motion for a human volunteer was used as a preliminary calculation of the skin motion of the face. For this calculation, a fiducial frame that attaches to a dental bite-block, the Locking Acrylic Dental Stent (LADS)[14] was used. The fiducial frame has acustar markers[3] attached to it. An infrared reference emitter was attached to the fiducial frame to compensate for the motion of the head during the acquisition of points. Figure 14 shows a picture of the fiducial frame, the reference emitter and the skin fiducials.

Seven skin fiducials were attached to the patient at different positions on the face. An optical tracker (Optotrak 3020 series, NDI Waterloo) with an infrared probe was used to localize the fiducials. The positions of the fiducials were localized eleven times per fiducial with varying random pressures applied on the fiducials during the fiducial localization. These moved the fiducials on the skin during the fiducial localization process. This was done to stimulate the possible fiducial motion that can happen during fiducial localization for image registration. The bone fiducials were also localized and these were used as a comparison to identify the maximum component of the error due to the optical localizer and the use of the reference emitter.

The mean of the 11 points per fiducial was calculated and the root mean square distances of those points from the mean was calculated. This was also done for the acustar fiducials.

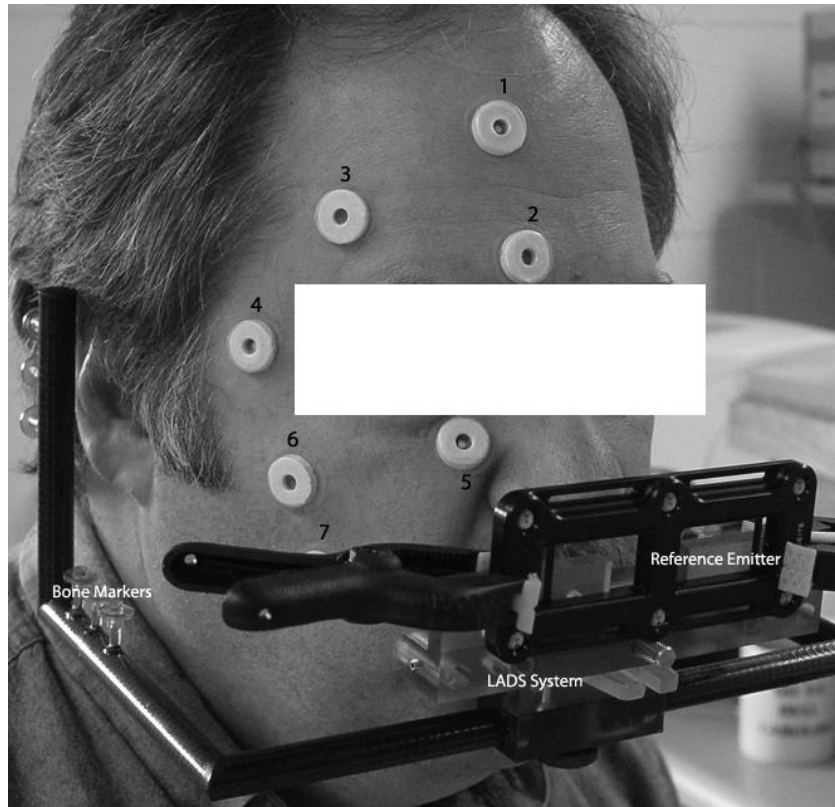


Figure 14: Picture of the face with the skin fiducials and the LADS with reference frame attached.

Sensitivity Analysis of effect of skin motions and errors in fiducial placement on the TRE in the target zone

Given that the bounds of the skin motion have been experimentally determined we could perform simulations. Skin motion was simulated by applying random vectors of different magnitudes on the fiducials. Random vectors were used because the preliminary data for the skin motion experiment showed that the fiducial measurements were uncorrelated in the both the x and the y dimensions. The random vectors were applied to both the optimized and the unoptimized fiducial positions. The random vectors encompass both the random and the biased motions of the skin because in some cases the skin may be moved in a biased way. The magnitude of the random vectors ranged from 1mm to 10mm. This range was found to be in accordance with the range of errors error obtained from the deviation of skin fiducial localized points from the mean of the data for each fiducial. The newly calculated fiducial position is then used to calculate the expected TRE in the target region. For the simulation, the fiducials are prevented from overlapping with each other but are allowed to be in any region around the face. This simulates the possible motion of the skin or the possible error of the localizer in localizing the position of the fiducials.

To simulate the effect of skin motion on the expected TRE in the target zone, 500 targets are chosen randomly in the target zone. The different fiducial positions produced by the random application of the errors of different magnitudes to both the initial and the final fiducials positions were used to calculate the TRE of all the 500 different targets in the target zone. For each skin motion magnitude, 1000 random vectors for the skin motion are calculated and added to both the optimized and the unoptimized fiducial positions. The average TRE for each magnitude is then calculated across the different random skin motion. The above procedure was

repeated with the optimized fiducial positions obtained from running the algorithm ten times. The average expected TRE across the different optimized fiducial results was then calculated.

Results

Figure 15a shows the result of the optimization algorithm. The squares are the initial fiducial positions and the round dots are the final fiducial positions. Figure 15b shows the point cloud of the skull phantom obtained from the laser range scan of the skull phantom face. The dark regions in Figure 15b are the taboo regions that are avoided during the optimization process but are included during the sensitivity analysis process. The mean value of the expected TRE for the 10 trials for the unoptimized fiducial configuration for FLE of 1mm was 0.81 ± 0.04 mm and was 1.62 ± 0.08 for FLE of 4mm. The mean values for the $\langle \text{TRE} \rangle$ for the 10 trials for the optimized fiducial position for an FLE of 1mm was 0.48 ± 0.01 mm and was 0.96 ± 0.02 for FLE of 4mm.

The results of the skin motion experiment are shown in table 9. The range of fiducial motion observed was from 1-8mm with the highest motion occurring in fiducial 7 which is located on the cheek. An average value of 0.21 ± 0.11 mm RMS error was found for the bone markers. This shows the error due to the optical localizer system used.



a



b

Figure 15: a) Skull phantom with the initial and final fiducial positions. The squares are the initial fiducial position and the circles are the final fiducial position. b) Laser range scan of the skull phantom with the taboo regions.

Table 9: The mean, standard deviation and the maximum values of the RMS distance of the localized fiducial points from the mean of the distances.

Fiducial	Mean(mm)	Standard Deviation (mm)	Maximum (mm)
1	1.37	0.64	2.35
2	3.60	1.52	6.21
3	2.45	1.09	3.95
4	3.25	1.23	4.90
5	4.09	1.57	6.75
6	4.12	0.94	6.01
7	5.40	1.79	8.21

Figure 16 shows the expected TRE of the target region for an FLE of 1mm for both the optimized and the unoptimized fiducial position. The mean values for the ten trials was obtained for the optimized fiducial location and plotted. From Figure 16 it can be observed that optimizing the fiducials lead to a reduction of the expected TRE in the target region by about 50%. Also the figure shows that the $\langle \text{TRE} \rangle$ increases more in the case of the unoptimized fiducial configuration when compared to the optimized fiducial configuration as the magnitude of the perturbation increases.

The standard deviation of the expected TRE in the unoptimized fiducial placement is larger than the standard deviation of the expected TRE values in the optimized fiducial case. This increase indicates an increase in the maximum observed TRE in the target region for the unoptimized fiducial. There is also an increase in the standard deviation of the TRE values in the unoptimized and optimized fiducial region as the magnitude of perturbation increases. Figure 17 shows the TRE calculated in the target region for an FLE of 4mm. The TRE increased as the FLE increased from 1 to 4mm. The expected TRE decrease from unoptimized to optimized fiducial position was still 50% and the standard deviation was still higher in the unoptimized vs. the optimized fiducial.

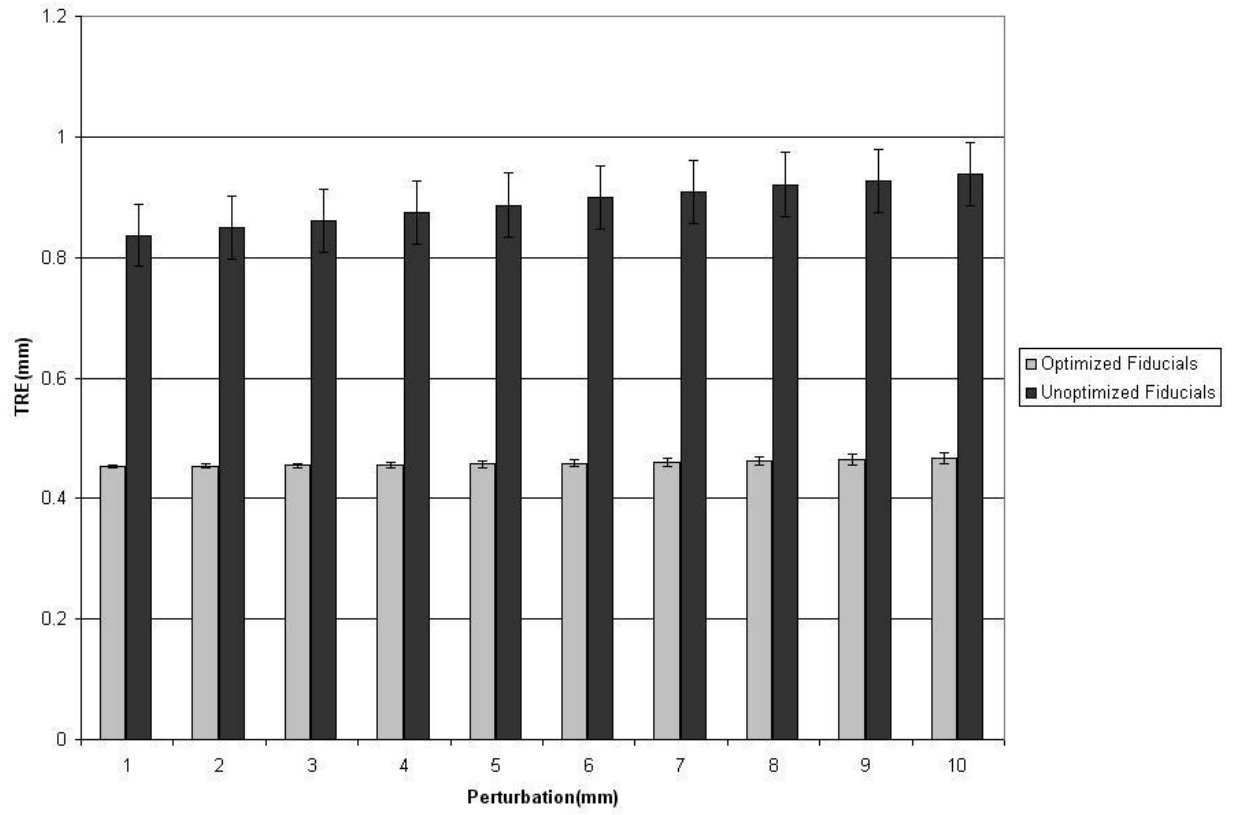


Figure 16: TRE calculated in the target region for FLE value of 1mm for an initial naïve initial fiducial position

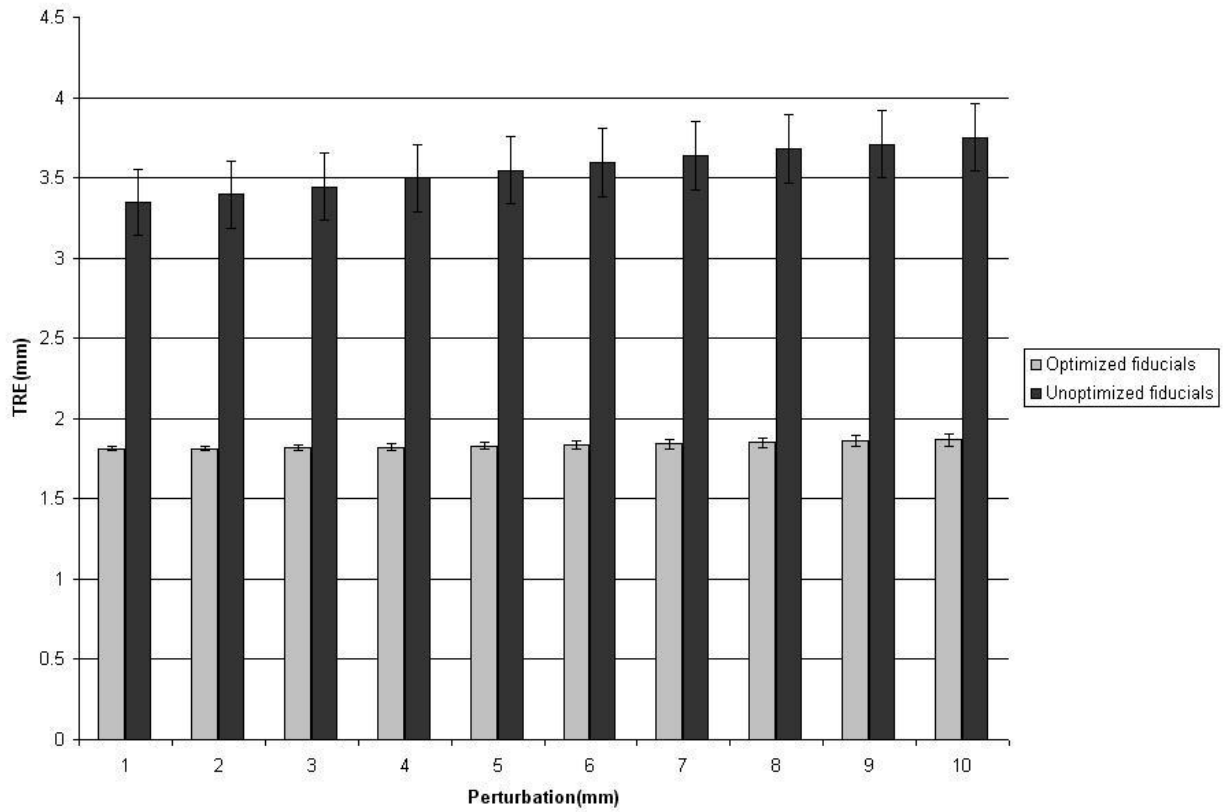


Figure 17: TRE calculated in the target region for FLE value of 4mm for an initial naïve initial fiducial position.

Since simulated annealing can produce different results for the same initial conditions, the simulated annealing algorithm was run ten times for different random placements of the fiducial and the sensitivity analysis of the region was done for the different results of the simulated annealing program.

The average TRE in the target region for the ten different runs for the simulated annealing program was calculated. Figure 18 shows the TRE of the region for the ten different runs of the simulated annealing program for an FLE of 1mm. From the figure, it can be observed that the simulated annealing program converges to roughly the fiducial placement that gives a similar TRE on the average in the target region. Also in all cases of the simulation the TRE obtained from the random motion was greater than the TRE from the optimized region and the TRE for the random placement varied widely between simulations with the TRE in a simulation nine as much 2.4 times the TRE of the optimized region.

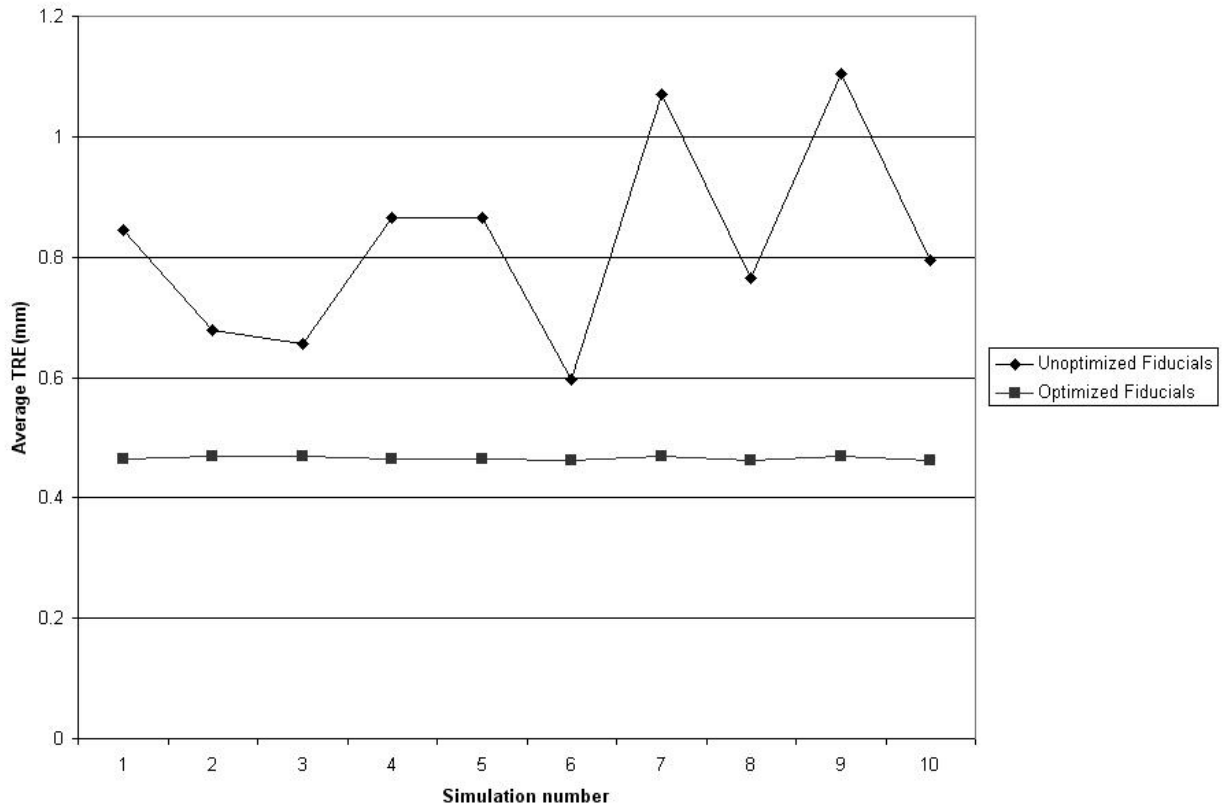


Figure 18: Average TRE in the target region for ten different simulations of the simulated annealing program

Discussion

In this paper, we developed a system to place fiducials on the surface of the face in order to improve the expected TRE and also reduce the sensitivity of small amounts of marker motion on the expected TRE in a target region. Boundaries on marker motion were set using experiments conducted on a human subject. These boundaries were then used to test the sensitivity of the optimized fiducial position to perturbations on the marker position. Simulated annealing was used to optimize the fiducial configuration because of its ability to avoid being trapped in local minima. The optimized fiducial configuration will be used for a magnetically tracked endoscopic transorbital procedure.

The algorithm developed produces an optimized fiducial position that is patient specific. It incorporates the surface structure of the patients, the taboo regions that encompass places that are most likely to move or regions that the physician wants unobstructed during the image acquisition process and the image guided procedure.

Skin fiducials although are more subject to motion than bone implanted fiducials, can provide adequate registration for frequently repeated procedure such as drug delivery to the optic nerve. The results show that regardless of the magnitude of the skin motion, an optimized fiducial placement will help reduce the effect of skin motion and the error in fiducial localization.

In this paper we used a phantom to study the effect of the optimization of fiducial position on the expected TRE in a target region. While this application is based on phantom data, we have used bounds developed from human data and plan to expand this test immediately into two areas. First we will use anthropomorphic phantoms with real targets to get true TRE and

second we will perform on cadavers for true anatomy. We also plan on working on a way to effectively place the fiducial on the skin after the fiducial positions are calculated.

References

1. West, J.B., et al., *Fiducial Point Placement and the Accuracy of Point-based, Rigid Body Registration*. Neurosurgery, 2001. **48**(4): p. 810-817.
2. Labadie, R.F., B.M. Davis, and M.J. Fitzpatrick, *Image-guided surgery: what is the accuracy*. Current opinion in Otolaryngology & Head and Neck Surgery, 2005. **13**: p. 27-31.
3. Maurer, C.R., Jr., et al., *Registration of head volume images using implantable fiducial markers*. IEEE Trans Med Imaging, 1997. **16**(4): p. 447-462.
4. Barnett, G.H., D.W. Miller, and J. Weisenberger, *Frameless stereotaxy with scalp-applied fiducial markers for brain biopsy procedures: experience in 218 cases*. Journal of Neurosurgery, 1999. **91**(4): p. 569-576.
5. Atuegwu, N., L. Mawn, and R.G. Jr, *Transorbital Image Guidance*, in *IEEE EMBS*. 2007: Lyon France.
6. Johann Hummel, et al., *Design and application of an assesment protocol for electromagnetic tracking systems*. Med Phys, 2005. **32**(7): p. 2371-2379.
7. Fitzpatrick, J.M., J.B. West, and C.R. Maurer, Jr., *Predicting error in rigid-body point-based registration*. Medical Imaging, IEEE Transactions on, 1998. **17**(5): p. 694.
8. Liu, H., et al., *Optimal marker placement in photogrammetry patient positioning system*. Medical Physics, 2002. **30**(2): p. 103-110.
9. Bohachevsky, I., O., M. Johnson, E., and M. Stein, L., *Generalized Simulated Annealing for Function Optimization*. Technometrics, 1986. **28**(3): p. 209-217.
10. Shechtman, D., et al., *Maximum Angle of Ocular Duction During Visual Fixation as a Function of Age*. Strabismus, 2004. **13**(1): p. 21.
11. Abramoff, M.D., W.J. Niessen, and M.A. Viergever, *Objective quantification of the motion of soft tissues in the orbit*. Medical Imaging, IEEE Transactions on, 2000. **19**(10): p. 986.
12. Dutton, J.J., *Atlas of Clinical and Surgical Orbital Anatomy*. 1994: W.B Saunders Company.

13. Jordan, D. and R. Anderson, *Surgical Anatomy of the Ocular Adnexa: A Clinical Approach*. Ophthalmology Monographs. 1996.
14. Labadie, R.F., et al., *Submillimetric target-registration error using a novel, non-invasive fiducial system for image-guided otologic surgery*. Computer Aided Surgery, 2004. **9**(4): p. 145-153.

CHAPTER V

MANUSCRIPT 3- Image guided transorbital endoscopic procedure in phantoms

Atuegwu N.C, Mawn L and Galloway R.L

Manuscript in review in IEEE Transaction in Biomedical Engineering.

Abstract

Transorbital endoscopic procedures are hindered by the visual similarity of orbital structures and that traditional orbital landmarks are lost during the procedure. These problems can be addressed with the use of image guidance.

Image guided transorbital endoscopic guidance was carried out in anthropomorphic phantoms. 5mm stellate balls were used for both the targets and as distracters. The targets were made radioopaque and attached to the orbit in close proximity to the distracters. White five mm stellate balls were used to mimic orbital fat and were used to obstruct the view of both the target and distracters. The targets were localized by three surgeons using a magnetic tracker attached to a flexible endoscope.

The surgeon with the highest skill level correctly identified the target 100% of the time. The fellow and the resident surgeons identified the targets correctly with image guidance 90% of the time and correctly without image guidance 70% of the time. The surgical attending and resident were faster with image guidance and the surgical fellow was equally as fast with image guidance. These results show a potential increase in accuracy and a decrease in time of the procedure by adding image guidance to transorbital procedures.

Introduction

Traditionally, access to the retrobulbar optic nerve required an orbitotomy; an invasive procedure in which either a rectus muscle is dissected from the globe or the lateral bony wall of the orbit is removed. Attempts to reduce the invasiveness of this procedure have been carried out with the use of an endoscope. Endoscopes were first used by Norris and Cleasby in the late 1970's for orbital surgery and later for orbital biopsies. They had an initial attempt at endoscopic guidance with a stereotaxic positioner to hold the endoscope at a fixed position but they had great difficulty with the stereotaxic arm and discontinued use [1-3].

More recently, Mawn, et al used a flexible endoscope to navigate the orbit for optic nerve sheath fenestration (ONSF). They reported that there were problems with navigation through the orbital cavity because the orbital structures were of similar color and also the traditional orbital landmarks were lost as the endoscope was moved through the orbit. They also reported that it took as much as 3 hours to complete an ONSF in a human cadaver [4].

Apart from the above state uses of the endoscope, new research on neuroprotection has brought to light additional potential uses of endoscope. Neuroprotection is the strategy of treating a disease by preventing neuronal cell death. Optic neuropathies, a group of diseases characterized by visual loss due to optic nerve dysfunction, are one of the main targets of neuroprotective therapy. The most common optic neuropathy is that associated with glaucoma. A number of factors can be responsible for optic neuropathy, but in all types of optic neuropathy, the injury is manifested at the optic nerve axon and results in the loss of retinal ganglion cells (RGCs) through apoptosis [5]. The new trend of thought is the potential of treating the optic nerve axon to prevent neuronal cell death.

Most of the common method of ocular drug deliveries do not effectively get the drugs to the optic nerve axon and may have additional side effects. A system that can guide an endoscope to the optic nerve for drug delivery can potentially be used for delivery of neuroprotective drugs to the optic nerve cells.

For orbital endoscopic procedures to be used, the problem of navigation through the orbital fat has to be improved since the orbital fat obscures easy visualization of optic nerve. This problem can be solved with the use of image guidance during the endoscopic procedure.

Image Guided Surgery and Interventions (IGS)

Image guided surgery and interventions involve the use of medical images to select, plan and guide a surgical procedure or medical intervention. Image guided surgery is based upon integration of the preoperatively acquired and processed 3D information such as an image volume of the patient and the corresponding anatomy of the patient within the same frame of reference. Links between these two components are realized by combining image space to patient space registration and by tracking instruments within the operational field.

The most common method of registration used for IGS is point based registration. Extrinsic point based registration requires fiducials attached to patients. Two basic types of fiducial markers are used in neurosurgical IGS: bone implantable markers [6] and skin surface fiducials [7]. Bone implanted fiducials, while providing greater accuracy, are more invasive and cannot be used for procedures that are repetitively done on a patient. Skin fiducials are not invasive and can be used frequently on a patient. We chose skin fiducials for our work because we envision the procedure being an outpatient procedure done multiple times a year and, as such, bone affixed fiducials will not be suitable. The fiducials are used to register the image space to

the physical space. After the registration of the two images, the surgical or interventional instruments have to be tracked within the operational field with a localizer.

Tracking a flexible endoscope in the operational field requires a localizer that does not rely on a line of site between the camera and the sensor. A Magnetic tracker offers this advantage and thus was selected for our work. Different groups have used magnetic trackers for imaging guided procedures [8-10]. This can be attributed to newer generations of electromagnetic trackers that show both an increased accuracy and have a reduced sensor size[11] making them easier to embed in instruments. A disadvantage of magnetic localizers is that they induce eddy currents in nearby conductive materials. These eddy currents create an opposing magnetic field to the original external magnetic field. The intersection of the Aurora's magnetic field with the opposing magnetic field disrupts the magnetic field and can affect the transformation data produced. This leads to systematic tracking errors. Careful placement of the magnetic transmitter and the magnetic sensor in relation to the metals in the environment can help reduce the amount of error in the measured position of the sensor[12]. There are several commercially available magnetic localizers and for this work the Aurora system (Northern Digital Inc, Waterloo, Ontario) was used.

Before a localizer can be effectively used for image guided procedures, a characterization of the localizer is required. A volumetric characterization of the FLE in the working volume of the Aurora magnetic tracker by sampling the magnetic field using a tomographic grid was performed by our lab [13]. The Aurora error characterization was performed by moving the flat plexi-glass phantom up in height in increments of 38.4mm from 9.6mm to 201.6mm. The final stopping distance was chosen to correspond to the average size of the human head. For each plane, a 5D and a 6D sensor was used to localize each divot and the random and the relative spatial FLE of

each plane was calculated. For different positions of the magnetic tracker from the object the random and spatial FLE was calculated. Different experimental setups shown in Figure 19 were proposed in our previous work[13]. For this paper we chose the setup in A shown in Figure 19. Based on the experimental setup A, the average random FLE was $0.034\pm 0.017\text{mm}$ for the 6D probe and $0.127\pm 0.063\text{mm}$ for the 5D probe and the average spatial FLE for the six planes is $0.40\pm 0.27\text{mm}$ for the 6D probe and $0.86\pm 0.42\text{mm}$ for the 5D probe. The effect of an endoscope on the flexible 5D magnetic sensor was also carried out by localizing a divot without and without the endoscope in contact with the sensor and measuring the deviation between the two measurements. The endoscope deviation was shown to be 0.2mm.

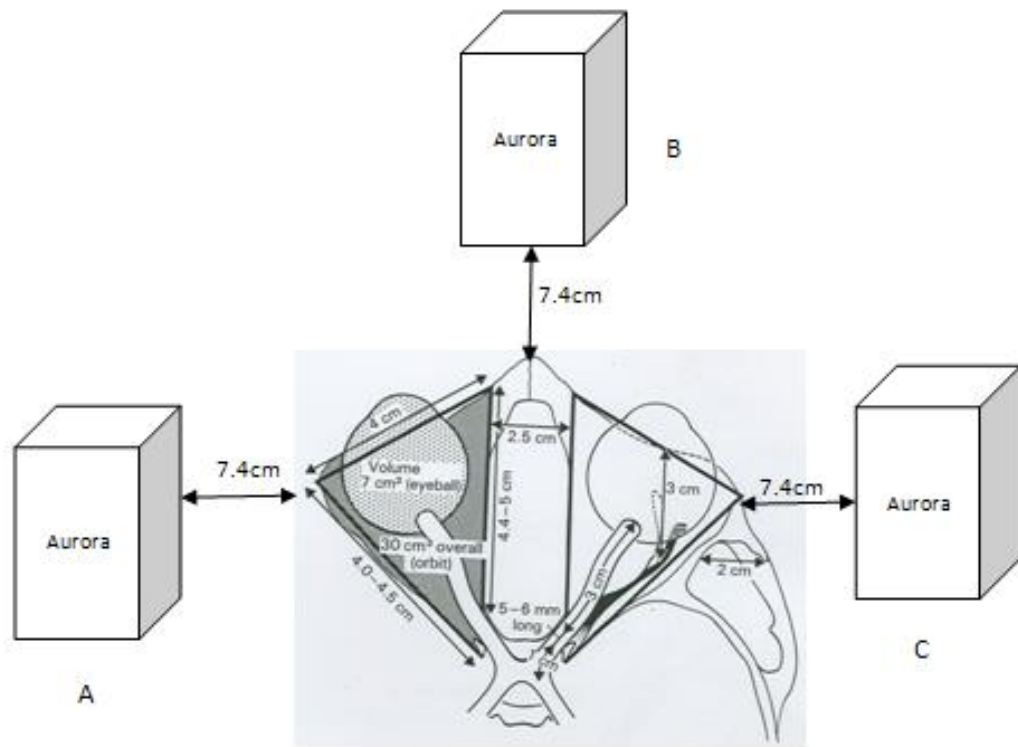


Figure 19: Picture of the possible placements of the magnetic tracker[13]

Methods

The retroorbital area is filled with fat which surrounds the optic nerve and cushions the eye. Targeting the optic nerve required penetration and transversal of the fat. The fat is confined by the orbital septum which shapes and structures the orbital fat. The orbital fat is deformable and can be penetrated. In order to have a penetrable material with a radiographically visible target, our experimental design was to use 5mm white stellate balls that were deformable, penetrable and visibly similar to fat as the orbital fat. We also used colored 5mm stellate balls soaked in iodine based computed tomography (CT) contrast agent as the target. The eyeballs and optic nerve were chosen based on size, distensibility and appearance to mimic their respective tissues. A nylon white cord was selected to mimic the optic nerve. The cord was soaked in iodine based CT contrast agent to make it radiopaque and was attached to the eyeball. The optic nerve-eyeball configuration was then attached to a skull through the optic foramen. Prior to soaking the targets in contrast agents, the target colors were randomly chosen from five possible colors and the positions of the targets in the orbit were randomly chosen based on the four quadrants of the orbit. Two additional colored balls were placed near the target to serve as distracters. The distracters colors were colors other than those chosen for the target. Colored targets and distracters were chosen to give color information to the endoscope and the radioactive target was chosen to give radioactive visibility to the target during the image guided procedure. The distracters were not soaked in iodine based contrast agent and as such were not visible on a CT volume. The targets and distracters were rigidly attached to the orbit with the use of white stellate balls attached to the bony orbit. This arrangement made the targets appear free floating and more difficult to get to. After the target and distracters were attached to the orbit the orbit was then filled up with the white stellate balls.



Figure 20: Picture of the experimental setup

Prior to the image guided (IG) procedure, skin fiducials were attached in an optimized manner on the phantoms [14] and a CT scan of the skull was obtained. Figure 20 shows a picture of the experimental setup with the eye of interest being the one closest to the Aurora magnetic tracker.

A point based registration algorithm was used for the registration of the fiducials positions in the image space and physical space. Image guidance was then performed using Operating Room Image Oriented Navigation (ORION) software[15]. ORION is a PC-based surgical guidance system which synchronously tracks and displays surgical position on up to four image sets and updates them in real time.

A 5D magnetic tracker was rigidly attached to a Storz Flex -X² (Karl Storz endoscopy America Inc) flexible endoscope. The endoscope-sensor configuration was used to localize the targets in the anthropomorphic phantoms. Prior to the target localization, the surgeons located the target in a CT image volume and are allowed to make calculations and take notes. The ORION four pane windows with three orthogonal views of the CT image in three planes and a view of the endoscopic image in one of the plane is used for the localization during the image guided part of the procedure. This is shown in Figure 21. For the non image guided part a stationary image with the target shown is available on a computer screen. The surgeon was allowed to consult the images during the procedure if they want clarification.

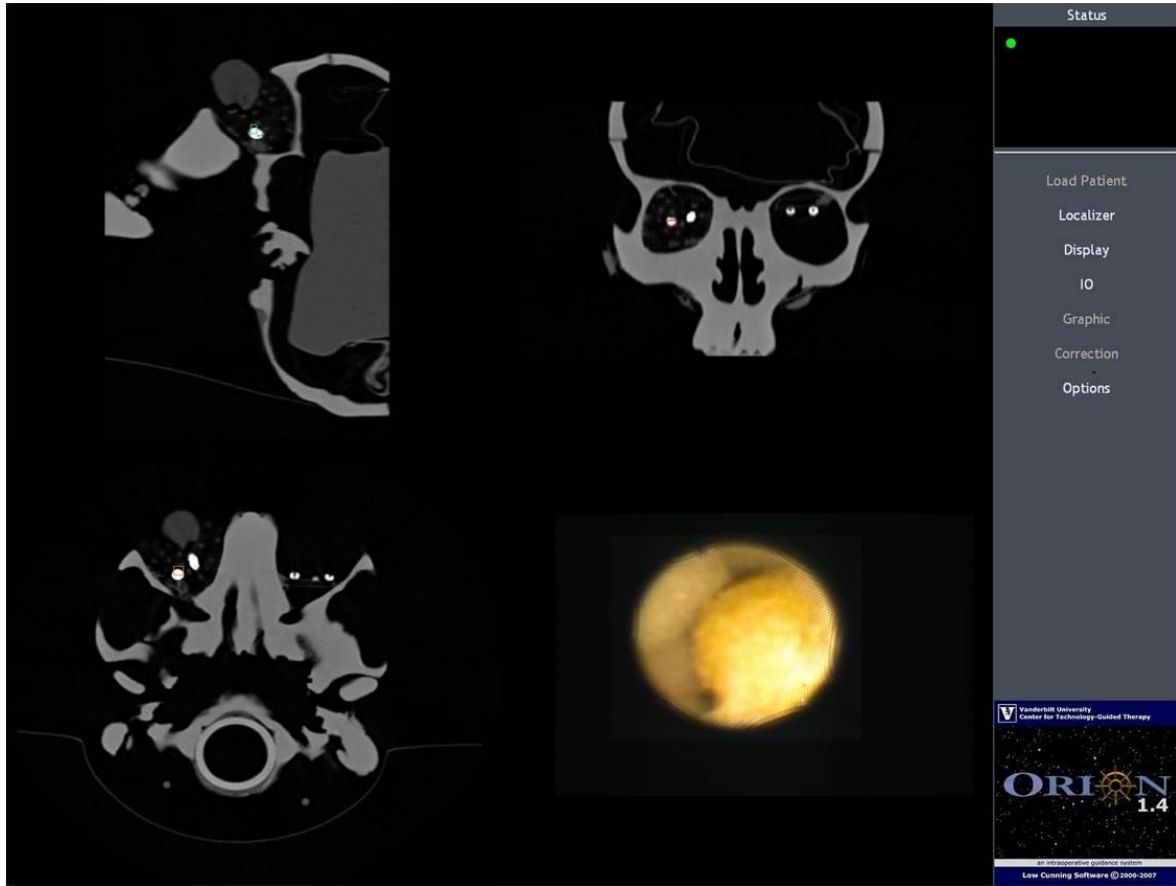


Figure 21: Screen shot of the ORION image guidance software used. The three planes show the three orthogonal views of the skull phantom and the last plane shows the endoscopic view.

The task for the surgeons was to identify the color of the target with and without image guidance. The time to target was recorded during the process. The order of surgeon experiment, image guided and non image guided was chosen randomly. The targets in the orbits were identified with either image guidance or non image guidance for the first trial. The opposite guided state was then applied in a second trial. The two trials for each target were separated by a week to prevent the surgeon from remembering the path to the target. The target correctness was neither confirmed nor denied during the whole experiment so the surgeon was not aware of the right answer. Twelve targets were localized by the attending surgeon (highest skill level), ten targets were localized by the surgical fellow and the surgical resident.

Results

Two metrics – percentage correct identification and time to target were used to evaluate the effect of image guidance. The times with the target correctly identified in both IG and non IG procedure is compared to determine the efficacy of image guidance for the three doctors with varying skill levels. Incorrect target identification is also recorded and analyzed. For the attending surgeon with the highest skill level the time to target with image guidance was on the average 2.5 times faster than the time to target without image guidance. The mean value for the time to target with image guidance was 72 seconds and the mean value of the time to target without image guidance was 163 seconds. The attending surgeon was able to locate the target correctly with both IG and non IG in 100% of the cases. Figure 22 shows a graph of the non image guided times vs. the image guided times. The line represents the time when image guidance is equal to non image guidance. Image guided times was faster in 83% of the times for the different target positions localized.

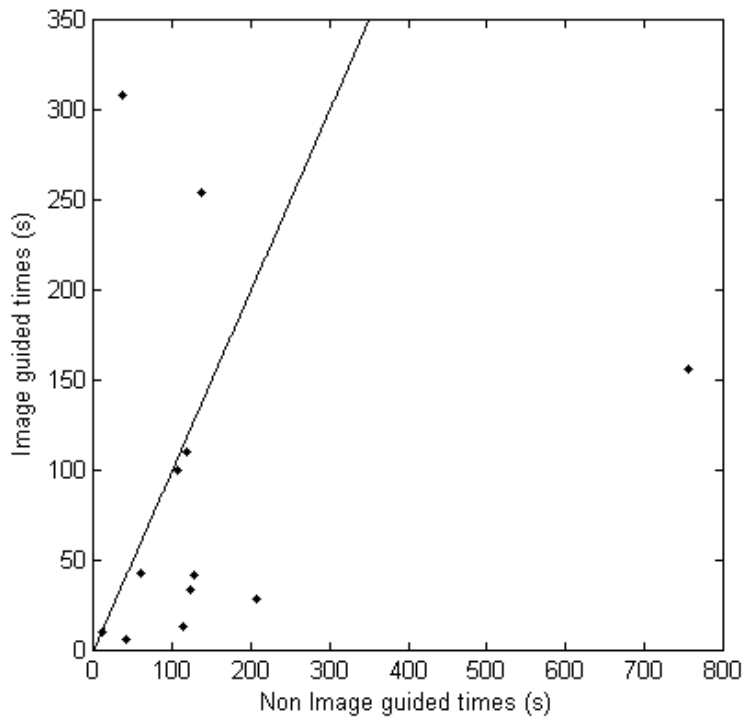


Figure 22: Graph of the non image guided times vs. the image guided times for the different targets for the attending surgeon. The line represents the times when the time to target with image guidance was equal to the time to target with non image guidance.

The results of the experiments for both the surgical resident and surgical fellow are shown in Figure 23 and Figure 24. The graph showed the times when the surgeons correctly identified the colored targets with both IG and non IG. The fellow and the resident surgeons correctly identified the target with image guidance 90% of the time and correctly identified the target with non image guidance 70% of the time. The fellow was faster with image guidance for the correct targets 50% of the times and the resident was faster with image guidance for the correct target 67% of the time. The results are summarized in Table 10.

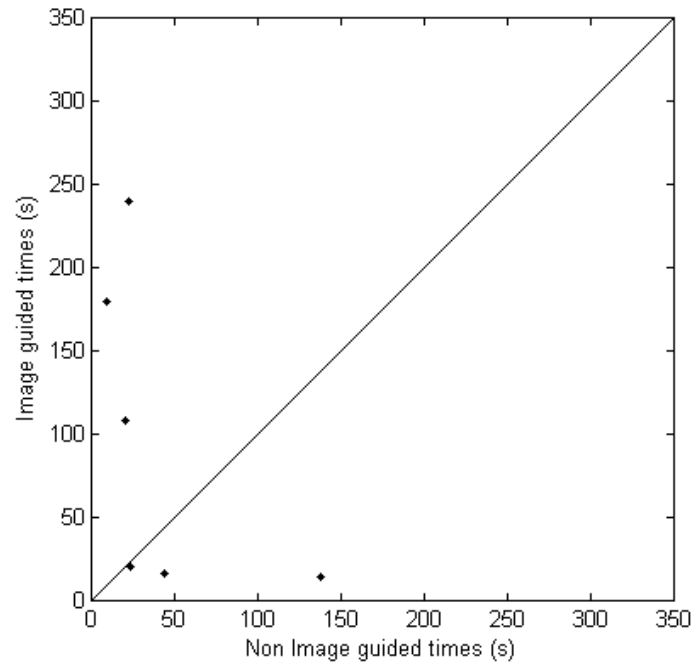


Figure 23: Graph of the non image guided times vs. the image guided times for the different targets for the surgical fellow.

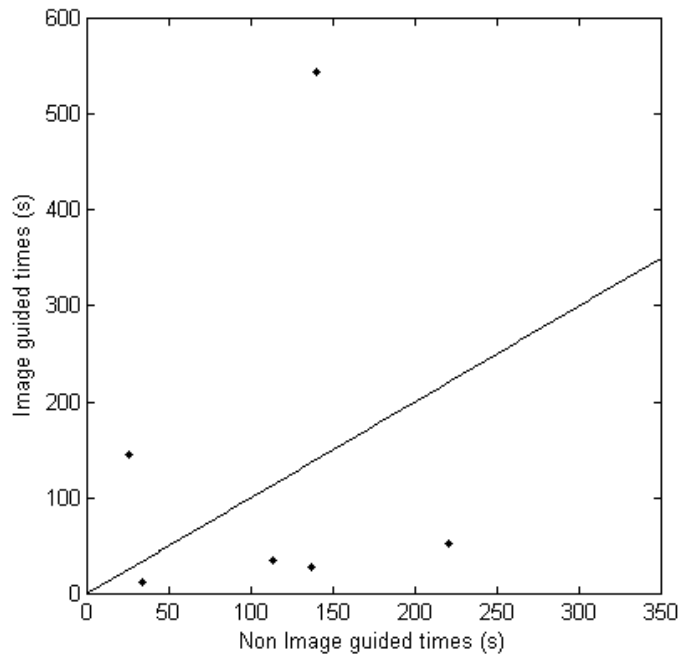


Figure 24: Graph of the non image guided times vs. the image guided times for the different targets for the surgical resident.

Table 10: The accuracy and the time of image guided and non image guided endoscopic phantom studies

Physician	% correct for image guidance	% correct for non image guidance	% of times that image guidance is faster
Attending	100	100	83
Fellow	90	70	50
Resident	90	70	67

Discussion

Transorbital endoscopic guidance was carried out on anthropomorphic phantoms. There was an increase in the accuracy of the procedure especially in less skilled surgeons with image guidance than without image guidance. Image guidance times were faster than non image guidance times in the case of the attending surgeon and the resident surgeon. It performed equally as fast as the non image guided times for the fellow. The discrepancy in the times found for different targets was due to the fact that the targets were different and randomly selected and this made some location was more difficult to get to than other location. Since the same target was identified with both image guidance and non image guidance, the difficulty level is same for the target but different across target. The above results show a potential benefit of image guided endoscopic transorbital procedures.

Acknowledgement

This work was supported by the NIH grant # 4-22-430-0713. The authors will like to thank Dr Cari Lyle and Dr Lillian Ringsdorf for their help with data collection. The authors will also like to thank Karl Storz endoscopy America Inc for providing us with the endoscope. The authors will also like to thank the CT tech in Vanderbilt medical center for help with imaging the phantoms.

References

1. Norris JL, C.G., *An endoscope for ophthalmology*. American Journal of Ophthalmology, 1978. **85**(3): p. 420-2.
2. Norris JL, S.W., *Bimanual endoscopic Orbital Biopsy*. Ophtalmology, 1985. **92**(1): p. 34-38.
3. Norris JL, C.G., *Endoscopic orbital surgery*. American Journal of Ophthalmology, 1981. **91**(2): p. 249-252.
4. Mawn, L.A.S., Jin-Hui ; Jordan, David R.; Joos, Karen M. , *Development of an Orbital Endoscope for Use with the Free Electron Laser*. Ophthalmic Plastic & Reconstructive Surgery, 2004. **20**(2): p. 150-157.
5. N Osborne, G.C., C J Layton, J P M Wood, R J Casson and J Melena, *Optic nerve and neuroprotection strategies*. Eye, 2004. **18**: p. 1075-1084.
6. Maurer, C.R., Jr., et al., *Registration of head volume images using implantable fiducial markers*. IEEE Trans Med Imaging, 1997. **16**(4): p. 447-462.
7. Barnett, G.H., D.W. Miller, and J. Weisenberger, *Frameless stereotaxy with scalp-applied fiducial markers for brain biopsy procedures: experience in 218 cases*. Journal of Neurosurgery, 1999. **91**(4): p. 569-576.
8. Zhang, H., et al., *Electromagnetic tracking for abdominal interventions in computer aided surgery*. Computer Aided Surgery, 2006. **11**(3): p. 127-136.
9. Wood, B.J., et al., *Navigation with Electromagnetic Tracking for Interventional Radiology Procedures: A Feasibility Study*. Journal of Vascular and Interventional Radiology, 2005. **16**: p. 493-505.
10. Krucker, J., et al., *Electromagnetic tracking for thermal ablation and biopsy guidance: clinical evaluation of spatial accuracy*. Journal of Vascular & Interventional Radiology, 2007. **18**(9): p. 1141-50.
11. Hummel, J.B., et al., *Evaluation of a new electromagnetic tracking system using a standardized assessment protocol*. Physics in Medicine and Biology, 2006. **51**: p. N205-N210.
12. Mark A. Nixon, B.C.M., W. Richard Fright and N. Brent Price, *The Effect of Metals and Interfering Fields on Electromagnetic Trackers*. Presence, MIT Press, 1998. **7**(2): p. 204-218.

13. Atuegwu, N.C. and R.L. Galloway, Jr, *Volumetric characterization of the Aurora magnetic tracker system for image guided transorbital endoscopic procedures*. Physics in Medicine and Biology, 2008.
14. Atuegwu, N.C. and R.L. Galloway, *Sensitivity analysis of fiducial placement on transorbital target registration error*. International Journal of Computer Assisted Radiology and Surgery, 2008. **2**(6): p. 397-404.
15. Stefansic, J.D., et al., *Design and implementation of a PC-based image-guided surgical system*. Computer Methods and Programs in Biomedicine 2002. **69**(3): p. 211-224.

CHAPTER VI

SUMMARY

Transorbital endoscopic procedures are hindered by the orbital fat that prevents direct visualization of the optic nerve. The addition of image guidance to transorbital procedures will help address this problem. With image-guidance orbital structures can be localized in the preoperatively obtained images and supplied to the surgeon via registration and an actively tracked tool. Such an image guidance system requires a registration between the physical space and the image space. A localizer is needed for both the registration and the tracking of the object after registration. For transorbital image guidance which requires non linear therapeutic paths, a non-line of sight system such as a magnetic localizer is most appropriate. Magnetic tracking systems have sensors that can be attached to the endoscopes to couple the live video with the location displayed on the preoperative images. While the most appropriate localizer for this application, magnetic localizers are inherently less accurate than optical localizers a volumetric characterization of the error metrics is required. Chapter III presents this volumetric characterization. The “sweet spot” of the magnetic tracker is documented and this is used in the placement of the magnetic tracker during endoscopic orbital procedures.

The registration accuracy metric, TRE, is affected by the placement of fiducials during the registration. Chapter IV presents the optimization of fiducials to reduce the TRE in a target region and the sensitivity analysis on the effect of fiducial localization error on the TRE. The bounds of the error were quantified by skin motion error calculations. The results of the optimization and the magnetic tracker characterization were used to quantify the benefits of adding image guidance to transorbital endoscopic procedure.

Chapter V presents the accuracy and the timing results of adding image guidance to transorbital endoscopic procedures in an anthropomorphic phantom. The results show that image guidance leads to a reduction of the time for the procedure and an increase in accuracy of the procedure. Also surgeons reported a greater confidence in their results with image guidance.

Future work with respect to the work presented here will be validating the effects of endoscopic image guidance in an animal model. The timing and accuracy in identifying targets have to be quantified. Also further validation of the reduction of TRE with the use of optimized fiducials has to be carried out both with phantoms and animals.

Appendix A

Accuracy measurement of the effect of some materials on the Aurora magnetic system

For image guided orbital endoscopic procedures, the role of the endoscope-magnetic sensor system is to mostly traverse the orbital fat. A measurement of the effect of fat and fat like materials on the sensor system is required in order to determine if there is error induced on the sensor position by the presence of fat and fatty substances.

Method

Three materials, steel, mayonnaise and animal fat were cut in lengths of 4cm and glued to a piece of wood. This prevents the movement of the materials during the measurement. A 5d sensor was rigidly attached to a plexiglass piece. Baseline measurements were done with the 5d sensors. The materials were then put within 5mm of the sensor and measurements were collected again. For both the baseline and the measurements with the material 1000 points were collected. The error due to the addition of the material was calculated by determining the difference of the mean of the two measurements (baseline and measurement with material). Baseline measurements were taken before any material was brought in close proximity to the sensor to ensure that any movement or shift in the sensor is recorded. This is essential to insure that any errors ascribed to the material were actually the result of the materials.

Results

The results of the experiment are shown in table 1 below. From table 1, the error due to steel is $1.7931e+005$ times more than the error due to animal fat. Also the error shown due to animal fat is very close to the baseline mean and within the random error of the sensor.

Table 11: Errors and variances due to the different materials

Material	Error(mm)	Variances	
		Baseline(mm ²)	Measurement with material(mm ²)
Steel	3.7606	0.0011	0.0016
Mayonnaise	4.6319e-005	0.0013	0.0015
Animal fat	2.0973e-005	9.2218e-004	0.0010

Discussion and conclusion

Since the deviation of the measurement with respect to the addition of fat is very small and within the random error of the sensor, then fat does not introduce any deviation in measured data versus those from measured in air. By using a material (steel) known to disturb the localization, we confirm the validity of the experiment. The difference in the errors observed for steel bolt and animal fat is due to the magnetic susceptibility of the two materials. Since the medical application exposes the localizer to fat, not steel, we have confidence that our phantom experiments with air based measurements predict the performance in patients.

APPENDIX B

Dealing with Correlated FLE

As seen in Chapter III, spatial FLE ($FLE_{spatial}$) is a slowly varying function of space. This means that there is in fact a strong correlation between the spatial component of FLE at each of the fiducial points and indeed at the target. Measured FLE is composed of a random term FLE_{random} and a spatial component of the FLE ($FLE_{spatial}$). However, the FLE/FRE/TRE theory developed by West and Fitzpatrick presumes that the FLE is uncorrelated across the measurement zone. $\langle TRE^2 \rangle = \langle FLE^2 \rangle \left(\frac{1}{N} + \frac{1}{K} \sum_{i=1}^K \sum_{j \neq i}^K \frac{r_i^2}{\Lambda_{ii}^2 + \Lambda_{jj}^2} \right)$ Thus the FLE used in the minimization algorithm in Chapter IV was the FLE_{random} . This is because the FLE has to be spatially uncorrelated for the equation above to hold true. However, changes in the $FLE_{spatial}$ also lead to changes in the TRE of the procedure. A quantification of the TRE increase due to $FLE_{spatial}$ is required to know the total TRE that is expected during the procedure.

Method

The $FLE_{spatial}$ measurements that were obtained in Chapter III were overlaid with the skull phantom used for the optimization method. The placement coincides with placement A shown in figure 1 below. The skull phantom and the grid phantom were overlaid as shown in figures 2 and 3. To calculate the FLE of the fiducials and the target centroid, the nearest plane to the centroid of the fiducials and the target and four the nearest grid points to the centroids of both the target and the fiducial in the nearest plane was used. This was done for 10 optimized and unoptimized fiducial positions and the translational TREs for the optimized fiducial positions were calculated. If we assume that the optic nerve will be at the centroid of the fiducial configuration then the

rotational TRE is negligible, then the TRE due to the $FLE_{spatial}$ will be the translational component of the TRE. The translational TRE due to $FLE_{spatial}$ is the difference between the average $FLE_{spatial}$, in each direction, at the fiducials, and the average $FLE_{spatial}$, in each direction, at the target.

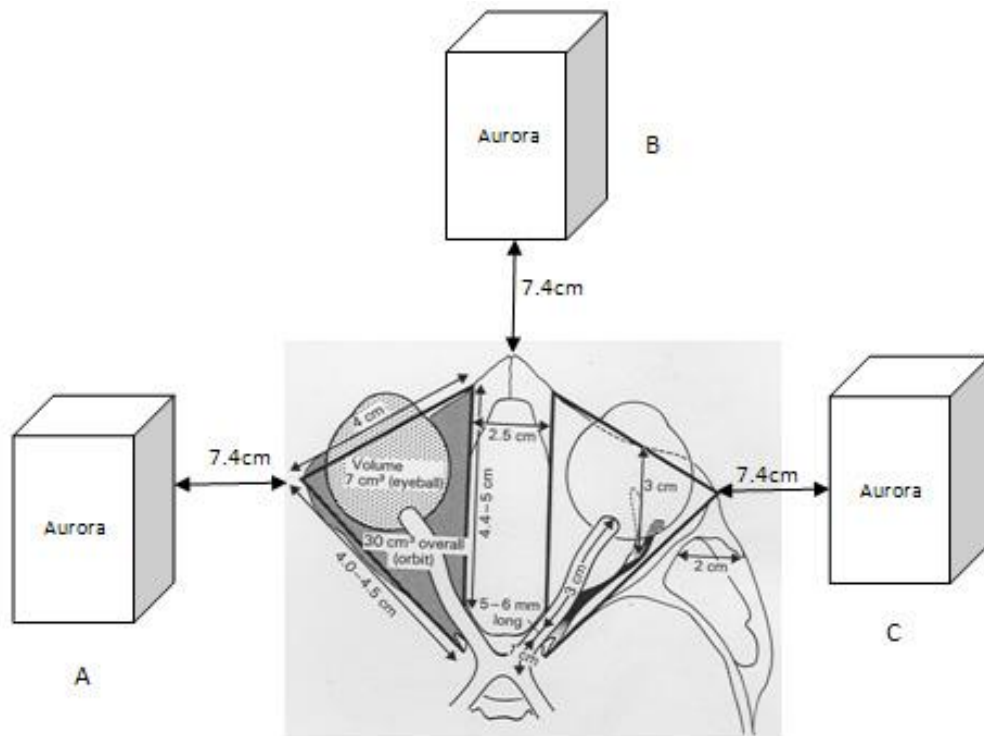


Figure 25: The possible placements of the Aurora magnetic tracker relative to the head.

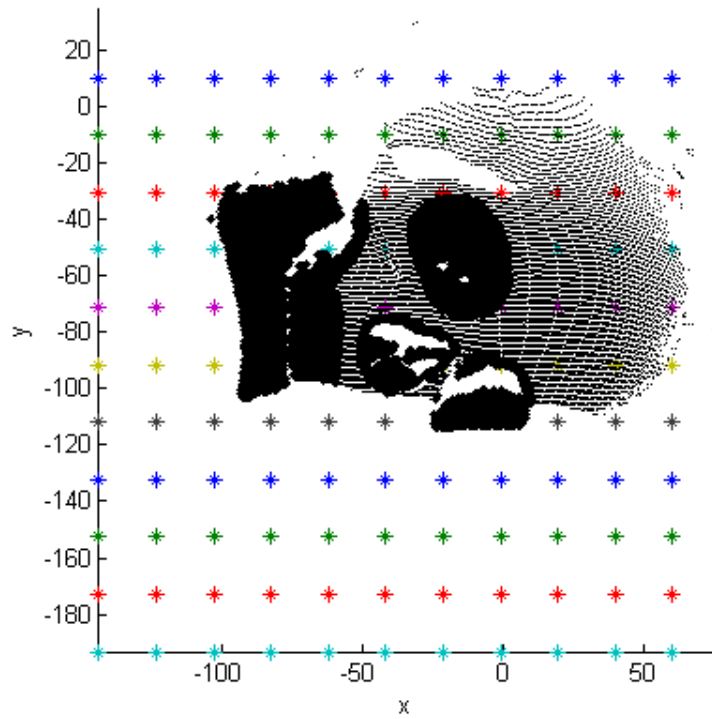


Figure 26: Overlay of the skull phantom and the grid phantom

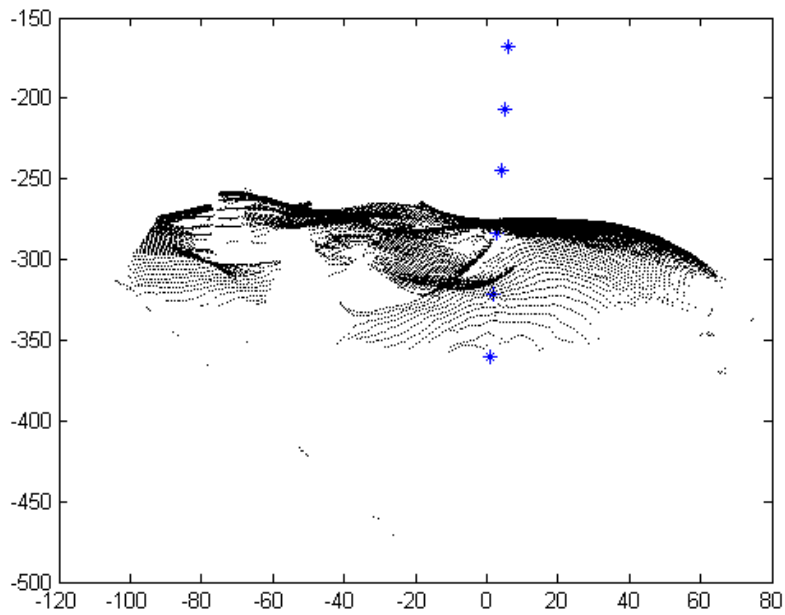


Figure 27: Planar overlay of the grid phantom and skull phantom

Results

Table 1 shows the translational TRE between the target and the fiducials for ten optimized trial runs. The average translational TRE is 0.2081 ± 0.1180 mm and the maximum and minimum translational TRE's are 0.3667mm and 0.0794mm respectively.

Table 12: Translational TRE values for the optimized fiducial configuration

Fiducial Configuration	1	2	3	4	5	6	7	8	9	10
TRE(mm)	0.361	0.140	0.367	0.114	0.122	0.321	0.322	0.108	0.080	0.148

Table 13: Translational TRE values for the unoptimized fiducial configuration

Fiducial Configuration	1	2	3	4	5	6	7	8	9	10
TRE(mm)	0.468	0.628	0.667	0.491	0.494	0.317	0.686	0.560	0.588	0.574

Table 2 shows the results of the translational TRE for the unoptimized trial runs. The average translational TRE is 0.547 ± 0.110 mm and the maximum and minimum translational TRE's are 0.686mm and 0.317mm respectively.

Discussion

The optimized fiducial placement leads to both a reduction in the TRE due to the random and $FLE_{spatial}$. The increase in the translational TRE in the unoptimized position may be due to the fact that the fiducials are placed in the region where the $FLE_{spatial}$ may be rapidly varying.