

**GOVERNMENT LEADERSHIP AND CENTRAL BANK DESIGN**

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# Abstract

## Government Leadership and Central Bank Design

This article investigates the impact on economic performance of the timing of moves in a policy game between the government and the central bank for a government with both distributional and stabilization objectives. It is shown that both inflation and income inequality are reduced without sacrificing output growth if the government assumes a leadership role compared to a regime in which monetary and fiscal policy is determined simultaneously. Further, it is shown that government leadership benefits both the fiscal and monetary authorities. The implications of these results for a country deciding whether to join a monetary union are also considered.

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## 1. Introduction

Over the past ten years, many countries have undertaken significant reforms in their monetary institutions. Most of these reforms have focused on providing central banks with a clear mandate to control inflation and greater responsibility for achieving the desired inflation performance. However, while there has been a common desire for improved inflation performance, countries vary widely in the institutional arrangements they have adopted to achieve this end. One of the fundamental differences between these new monetary institutions is the degree to which the government assumes a leadership role in determining the objectives of monetary policy. Our purpose, in this article, is to determine whether government leadership can be expected to have a positive or negative impact on economic performance.

Weymark's (2001) model of monetary policy delegation provides the theoretical framework for our analysis. In this model, the optimal institutional design, defined in terms of central bank independence and conservatism, is the outcome of a two-stage non-cooperative game between the the government and the central bank. In the first stage of the game, the government appoints a central banker and chooses how much independence to grant the central bank. In the second stage, the central bank and the government move simultaneously; the government sets government expenditures and transfer payments and the central bank sets the size of the money supply.

The model that Weymark employs is a better representation of the monetary institutions in some countries than in others. The strategic interaction between the European Central Bank (ECB) and the governments of EMU members, for example, is probably best approximated by a game in which the ECB and national fiscal authorities are engaged in a non-cooperative, simultaneous move game. However, the institutional arrangements that have been adopted in other countries, in particular Canada, New Zealand, and the United Kingdom, are characterized by a significant degree of government leadership. Governments that can exert influence over monetary policy are likely to take this into account when formulating their fiscal policies. In order to capture this aspect of government leadership, we amend Weymark's model

to allow the government to play the role of Stackelberg leader in the second stage of the policy game. We also assume that the central bank's inflation target is established (exogenously) by government mandate.

In our model, the government chooses an optimal institutional design, conditional on the impact that alternative institutional arrangements are expected to have on its own fiscal policies and the central bank's monetary policy. Because problems of institutional design necessarily apply to longer-term horizons, the fiscal and monetary policies that we consider are best viewed as long-term policy responses, rather than short-term demand management tools. A comparison of the theoretical results of our analysis here with those obtained by Weymark (2001) shows that government leadership improves inflation performance and enhances income redistribution without sacrificing output growth. Furthermore, these improvements in economic performance benefit both the monetary and fiscal authorities.<sup>1</sup>

In order to assess whether our results are of practical importance, we calculate the losses associated with the two policy regimes, simultaneous moves and government leadership, for nine countries: Canada, France, Germany, Italy, New Zealand, Sweden, Switzerland, the United Kingdom, and the United States. When we express our measure of welfare in output equivalent units, we find that the benefits of government leadership are equivalent to a permanent increase of 1–2 percent in the long run growth rate for all countries. This result is of particular significance to the United Kingdom, which currently has monetary institutions that confer a leadership role on its government. If the UK were to join the Eurozone, government leadership in monetary policy formation would have to be relinquished.

## 2. Economic Structure

The model used in Weymark (2001) provides a useful framework for the present

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<sup>1</sup>In the literature on policy coordination, institutional arrangements that lead to Pareto improvements relative to the Cournot-Nash equilibrium are viewed as coordination devices. See, for example, Hughes Hallett (1998).

analysis. For purposes of exposition, we suppress potential spillover effects between countries and focus on the following three equations to represent the economic structure of any country:

$$\pi_t = \pi_t^e + \alpha y_t + u_t \quad (1)$$

$$y_t = \beta(m_t - \pi_t) + \gamma g_t + \epsilon_t \quad (2)$$

$$g_t = m_t + s(by_t - \tau_t) \quad (3)$$

where  $\pi_t$  is the inflation rate in period  $t$ ,  $y_t$  is output growth in period  $t$ , and  $\pi_t^e$  represents the rate of inflation that rational agents expect will prevail in period  $t$ , conditional on the information available at the time expectations are formed. The variables  $m_t$ ,  $g_t$ , and  $\tau_t$  represent, respectively, the growth in the money supply, government expenditures, and tax revenues in period  $t$ . The variables  $u_t$  and  $\epsilon_t$  are random disturbances which are assumed to be independently distributed with zero mean and constant variance. The coefficients  $\alpha, \beta, \gamma, s$ , and  $b$  are all positive by assumption. The assumption that  $\gamma$  is positive may be considered controversial.<sup>2</sup> However, short-run impact multipliers derived from Taylor's (1993) multi-country estimation provide empirical support for this assumption.<sup>3</sup>

According to (1), inflation is increasing in the rate of inflation predicted by private agents and in output growth. Equation (2) indicates that both monetary and fiscal policies have an impact on the output gap. The microfoundations of the aggregate supply equation (1), originally derived by Lucas (1972, 1973), are well-known. Mc-

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<sup>2</sup>Barro (1981) argues that government purchases have a contractionary impact on output. However, in contrast to those who argue that fiscal policy has little systematic or positive impact on economic performance, our model treats fiscal policy as important because (i) fiscal policy is used by governments to achieve includes redistributive objectives whose consequences need to be taken into account and (ii) as Dixit and Lambertini (2001) point out, governments cannot precommit monetary policy with any credibility if fiscal policy is not also precommitted.

<sup>3</sup>For example, using Taylor's empirical results, Hughes Hallett and Weymark (2002) obtain short-run  $\gamma$  estimates of 0.57, 0.43, 0.60, and 0.58 for France, Germany, Italy, and the United Kingdom, respectively.

Callum (1989) shows that aggregate demand equations like (2) can be derived from a standard, multiperiod utility-maximization problem.

Equation (3) describes the government's budget constraint. In the interests of simplicity, we allow discretionary tax revenues to be used for redistributive purposes only. Thus, in each period, the government must finance its remaining expenditures by selling government bonds to the central bank or to private agents.<sup>4</sup> We assume that there are two types of agents, rich and poor, and that only the rich use their savings to buy government bonds. In (3),  $b$  is the proportion of pre-tax income (output) that goes to the rich and  $s$  is the proportion of after-tax income that the rich allocate to saving. The tax,  $\tau_t$ , is used by the government to redistribute income from the rich to the poor.

Using (1) and (2) to solve for  $\pi_t^e$ ,  $\pi_t$  and  $y_t$  yields the following reduced forms:

$$\pi_t(g_t, m_t) = (1 + \alpha\beta)^{-1}[\alpha\beta m_t + \alpha\gamma g_t + m_t^e + \frac{\gamma}{\beta}g_t^e + \alpha\epsilon_t + u_t] \quad (4)$$

$$y_t(g_t, m_t) = (1 + \alpha\beta)^{-1}[\beta m_t + \gamma g_t - \beta m_t^e - \gamma g_t^e + \epsilon_t - \beta u_t]. \quad (5)$$

Equations (5) and (3) then imply

$$\begin{aligned} \tau_t(g_t, m_t) = [s(1 + \alpha\beta)]^{-1} & [(1 + \alpha\beta + sb\beta)m_t - (1 + \alpha\beta - sb\gamma)g_t \\ & - sb\beta m_t^e - sb\gamma g_t^e + sb\epsilon_t - sb\beta u_t] \end{aligned} \quad (6)$$

### 3. Government and Central Bank Objectives

In our formulation, we allow for the possibility that the government and a fully independent central bank may differ in their objectives in some significant way. In particular, we assume that the government cares about inflation stabilization, output

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<sup>4</sup>Several variations which relax the restrictions on how fiscal policy may be financed are considered in Weymark (2001). Specifically, in one variation, bond financing is replaced by income taxes which can be used to finance both  $g_t$  and  $\tau_t$ . In another variation, income taxes and newly-created general taxes are available to finance  $g_t$  and  $\tau_t$ . However, the model's theoretical predictions are robust to these variations.

growth, and income redistribution, whereas the central bank, if left to itself, would be concerned only with the first two objectives.<sup>5</sup> We also assume that the government has been elected by majority vote, so that the government's loss function reflects society's preferences over alternative economic objectives.

Formally, the government's loss function is given by

$$L_t^g = \frac{1}{2}(\pi_t - \hat{\pi})^2 - \lambda_1^g y_t + \frac{\lambda_2^g}{2}[(b - \theta)y_t - \tau_t]^2 \quad (7)$$

where  $\hat{\pi}$  is the government's inflation target,  $\lambda_1^g$  is the relative weight that the government assigns to output growth, and  $\lambda_2^g$  is the relative weight assigned to income redistribution. The parameter  $\theta$  represents the proportion of output that the government would, ideally, like to allocate to the rich. All other variables are as previously defined.

The first term on the right-hand side of (7) reflects the government's concern with inflation stabilization. Specifically, the government incurs losses when actual inflation deviates from the inflation target. The second term is intended to capture what many believe is a political reality for governments—namely, that voters reward governments for increases in output growth and penalize them for reductions in the growth rate.<sup>6</sup> The third component in the government's loss function reflects the government's concern with income redistribution. The parameter  $\theta$  represents the government's ideal degree of income inequality. For example, in an economy in which there are as many rich people as poor people, an egalitarian government would set

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<sup>5</sup>The assumption that a fully independent central bank assigns a zero weight to income redistribution simplifies the algebra involved in solving the policy game without having any significant impact on the qualitative results.

<sup>6</sup>In adopting a linear representation of the output objective, we follow Barro and Gordon (1983). In the monetary delegation literature, the output component in the government's loss function is more often represented as quadratic because the models employed typically preclude any stabilization role for monetary policy when the output term in the loss function is linear. In our model, the quadratic income redistribution term in the loss function allows monetary policy to play a role in output stabilization.



$\theta = 0.5$ . Ideally, in this case, the government would like to redistribute output in the amount of  $(b - 0.5)y_t$  from the rich to the poor.

We characterize the objectives of the central bank, which are distinct from those of the government, as:

$$L_t^{cb} = \frac{1}{2}(\pi_t - \hat{\pi})^2 - (1 - \delta)\lambda^{cb}y_t - \delta\lambda_1^g y_t + \frac{\delta\lambda_2^g}{2}[(b - \theta)y_t - \tau_t]^2 \quad (8)$$

where  $0 \leq \delta \leq 1$ , and  $\lambda^{cb}$  is the weight that the central bank assigns to output growth. The parameter  $\delta$  measures the degree to which the central bank is forced to take the government's objectives into account when formulating monetary policy. The closer  $\delta$  is to 0, the greater is the independence of the central bank.

In (7) we have described  $\hat{\pi}$  as the government's inflation target. The fact that the same inflation target appears in (8) reflects our assumption that the central bank has instrument independence but not target independence.

## 4. The Policy Game

We characterize the strategic interaction between the government and the central bank as a two-stage non-cooperative game in which the structure of the model and the objective functions are common knowledge. In the first stage, the government chooses the institutional parameters  $\delta$  and  $\lambda^{cb}$ . The second stage is a Stackelberg game in which the government takes on the leadership role. In the second stage, the government and the monetary authority set their policy instruments, given the  $\delta$  and  $\lambda^{cb}$  values determined at the previous stage. Private agents understand the game and form rational expectations for future prices in the second stage. Formally, the policy game can be described as follows:

### Stage 1

The government solves the problem:

$$\min_{\delta, \lambda^{cb}} E L^g(g_t, m_t, \delta, \lambda^{cb}) = E \left\{ \frac{1}{2}[\pi_t(g_t, m_t) - \hat{\pi}]^2 - \lambda_1^g [y_t(g_t, m_t)] + \frac{\lambda_2^g}{2} [(b - \theta)y_t(g_t, m_t) - \tau_t(g_t, m_t)]^2 \right\} \quad (9)$$

where  $L^g(g_t, m_t, \delta, \lambda^{cb})$  is (7) evaluated at  $(g_t, m_t, \delta, \lambda^{cb})$ , and  $E$  is the expectations operator.

## Stage 2

- (i) Private agents form rational expectations about future prices  $\pi_t^e$  before the shocks  $u_t$  and  $\epsilon_t$  are realized.
- (ii) The shocks  $u_t$  and  $\epsilon_t$  are realized and observed by the government and by the central bank.
- (iii) The government chooses  $g_t$ , before  $m_t$  is chosen by the central bank, to minimize  $L^g(g_t, m_t, \bar{\delta}, \bar{\lambda}^{cb})$ , where  $\bar{\delta}$  and  $\bar{\lambda}^{cb}$  indicates that these variables were determined in stage 1.
- (iv) The central bank chooses  $m_t$ , taking  $g_t$  as given, to minimize

$$L^{cb}(g_t, m_t, \bar{\delta}, \bar{\lambda}^{cb}) = \frac{(1 - \bar{\delta})}{2} [\pi_t(g_t, m_t) - \hat{\pi}]^2 - (1 - \bar{\delta}) \bar{\lambda}^{cb} [y_t(g_t, m_t)] + \bar{\delta} L^g(g_t, m_t, \bar{\delta}, \bar{\lambda}^{cb}) \quad (10)$$

The timing of our two-stage game is illustrated in Figure 1.

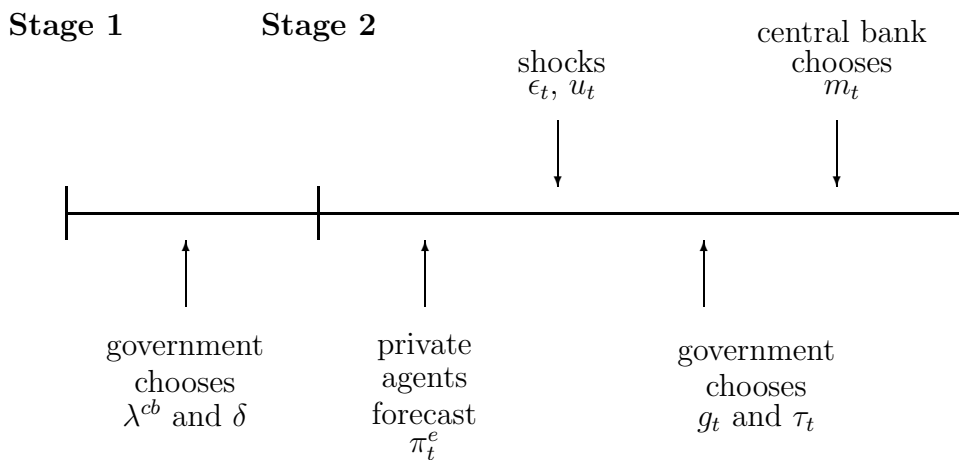


Figure 1: The Stages and Timing of the Policy Game

This game can be solved by first solving the second stage of the problem for the optimal money supply and government expenditure policies with  $\delta$  and  $\lambda^{cb}$  fixed, and then solving stage 1 by substituting the stage 2 results into (9) and minimizing with respect to  $\delta$  and  $\lambda^{cb}$ . The equilibrium for the stage 2 leader-follower game is:

$$\begin{aligned}
m_t(\delta, \lambda^{cb}) &= \frac{\beta \hat{\pi}}{(\beta + \gamma)} + \frac{(1 - \delta)\beta[\beta(\phi - \eta\Lambda)\lambda_2^g + \alpha\gamma(\beta\eta + \gamma)s^2]\lambda^{cb}}{\alpha(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} \\
&+ \frac{\delta\beta[\beta\phi + \gamma\Lambda]\lambda_1^g}{\alpha(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]} - \frac{(1 - \gamma\theta s)u_t}{\alpha(\beta + \gamma)} \\
&- \frac{(1 - \delta)\beta\gamma s^2(\beta\eta + \gamma)\lambda_1^g}{(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} - \frac{\epsilon_t}{(\beta + \gamma)} \tag{11}
\end{aligned}$$

$$\begin{aligned}
g_t(\delta, \lambda^{cb}) &= \frac{\beta \hat{\pi}}{(\beta + \gamma)} + \frac{(1 - \delta)\beta^2[(\phi - \eta\Lambda)\lambda_2^g - \alpha s^2(\beta\eta + \gamma)]\lambda^{cb}}{\alpha(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} \\
&+ \frac{\delta\beta[\beta\phi + \gamma\Lambda]\lambda_1^g}{\alpha(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]} - \frac{(1 + \beta\theta s)u_t}{\alpha(\beta + \gamma)} \\
&+ \frac{(1 - \delta)(\beta s)^2(\beta\eta + \gamma)\lambda_1^g}{(\beta + \gamma)[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} - \frac{\epsilon_t}{(\beta + \gamma)} \tag{12}
\end{aligned}$$

where

$$\eta = \frac{\partial m_t}{\partial g_t} = \frac{-\alpha^2\gamma\beta s^2 + \delta\phi\Lambda\lambda_2^g}{(\alpha\beta s)^2 + \delta\Lambda^2\lambda_2^g} \tag{13}$$

$$\phi = 1 + \alpha\beta - \gamma\theta s \tag{14}$$

$$\Lambda = 1 + \alpha\beta + \beta\theta s. \tag{15}$$

Taking the mathematical expectation of both sides of (11) and (12) to obtain  $m_t^e$  and  $g_t^e$ , respectively, and substituting the result, together with (11) and (12), into (4) and (5) yields the reduced-form solutions for  $\pi_t$  and  $y_t$  as functions of the institutional variables  $\delta$  and  $\lambda^{cb}$

$$\pi_t(\delta, \lambda^{cb}) = \hat{\pi} + \frac{(1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g}{\alpha[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]} \tag{16}$$

$$y_t(\delta, \lambda^{cb}) = \frac{-u_t}{\alpha}. \quad (17)$$

From (6), the reduced-form solution for  $\tau_t$  is given by

$$\tau_t(\delta, \lambda^{cb}) = \frac{(1-\delta)\beta s(\beta\eta + \gamma)(\lambda^{cb} - \lambda_1^g)}{[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} - \frac{(b-\theta)u_t}{\alpha}. \quad (18)$$

Substituting (16)–(18) into (9), the government's stage 1 minimization problem can be expressed as

$$\begin{aligned} \min_{\delta, \lambda^{cb}} EL^g(\delta, \lambda^{cb}) &= \frac{1}{2} \left\{ \frac{(1-\delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g}{\alpha[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]} \right\}^2 \\ &+ \frac{\lambda_2^g}{2} \left\{ \frac{(1-\delta)\beta s(\beta\eta + \gamma)(\lambda^{cb} - \lambda_1^g)}{[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]\lambda_2^g} \right\}^2. \end{aligned} \quad (19)$$

Partial differentiation of (19) with respect  $\lambda^{cb}$  and  $\delta$  yields the first-order conditions

$$\begin{aligned} \frac{\partial EL^g(\delta, \lambda^{cb})}{\partial \lambda^{cb}} &= \frac{[(1-\delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g](1-\delta)\beta(\phi - \eta\Lambda)}{\alpha^2[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]^2} \\ &- \frac{(1-\delta)^2(\beta s)^2(\beta\eta + \gamma)^2(\lambda_1^g - \lambda^{cb})}{\lambda_2^g[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]^2} = 0 \end{aligned} \quad (20)$$

$$\begin{aligned} \frac{\partial EL^g(\delta, \lambda^{cb})}{\partial \delta} &= \frac{(1-\delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g\beta[\beta\phi + \gamma\Lambda]}{\alpha^2[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]^3} \\ &- \frac{(1-\delta)(\beta\eta + \gamma)(\beta s)^2[\beta\phi + \gamma\Lambda]}{\lambda_2^g[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]^3} \\ &\frac{\{(\beta\eta + \gamma) - (1-\delta)\beta\Omega\}(\lambda_1^g - \lambda^{cb})^2}{\lambda_2^g[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)]^3} = 0 \end{aligned} \quad (21)$$

where  $\Omega = \partial\eta/\partial\delta$ .

It is evident that  $[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)] = 0$  is not a solution to the minimization problem. When  $[\beta(\phi - \eta\Lambda) + \delta\Lambda(\beta\eta + \gamma)] \neq 0$ , (20) and (21) yield, respectively, (22) and (23):

$$(1 - \delta)(\phi - \eta\Lambda)\lambda_2^g \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} - (1 - \delta)^2(\beta\eta + \gamma)^2(\alpha s)^2\beta(\lambda_1^g - \lambda^{cb}) = 0 \quad (22)$$

$$\begin{aligned} & \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} (\lambda_1^g - \lambda^{cb}) \\ & \quad \{ \delta(1 - \delta)\Lambda\Omega + (\phi - \eta\Lambda) \} \lambda_2^g \\ & - (1 - \delta)(\beta\eta + \gamma)(\alpha s)^2\beta \{ (\beta\eta + \gamma) - (1 - \delta)\beta\Omega \} (\lambda_1^g - \lambda^{cb})^2 = 0. \end{aligned} \quad (23)$$

There are two real-valued solutions that satisfy the first-order conditions given above and which fall within the permissible range for  $\delta$ .<sup>7</sup> By inspection, it is apparent that (22) and (23) are both satisfied when  $\delta = 1$  and  $\lambda^{cb} = \lambda_1^g$ . This solution characterizes a central bank that is fully dependent. The second real-valued solution is  $\delta = \lambda^{cb} = 0$ . In this case, the central bank is fully independent and exclusively concerned with the economy's inflation performance.

The solution that yields the minimum loss for the government, as measured by the government's loss function (7), can be identified by using (19) to compare the expected loss that would be suffered under the alternative institutional arrangements. Substituting  $\delta = 1$  and  $\lambda^{cb} = \lambda_1^g$  into (19) results in

$$EL^g = \frac{(\lambda_1^g)^2}{2\alpha^2}. \quad (24)$$

Substituting  $\delta = \lambda^{cb} = 0$  into the right-hand-side of (19) yields

$$EL^g = 0. \quad (25)$$

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<sup>7</sup>Because  $\eta$  is a function of  $\delta$ , (23) is a quartic polynomial in  $\delta$ . This polynomial has four distinct roots, of which only two are real-valued. Details of the complete solution set for the first-order conditions may be found in Appendix 1.

It is evident that when institutional arrangements are such that the government is the Stackelberg leader in the second stage policy game, the optimal central bank design, from society's point of view, is one in which the central bank is required to use monetary policy to achieve the government's chosen inflation target and is granted full independence to do so. As we show in Appendix 2, central bank leadership does not provide as good a result from the government's point of view, *even if* the government dictates the inflation target.

Our results show that when there is government leadership, society's welfare, as measured by the inverse of (19), is maximized when the government appoints central bankers who are concerned only with the achievement of the mandated inflation target, and completely disregard the impact that their policies may have on output growth. However, our results also indicate that full central bank independence is beneficial under more general conditions. When  $\delta = 0$ ,  $\beta\eta + \gamma = 0$ , and (19) is given by

$$EL^g = \frac{1}{2} \left\{ \frac{\lambda^{cb}}{\alpha} \right\}^2 \quad (26)$$

for any arbitrary value of  $\lambda^{cb}$ , when  $\delta = 0$ . Clearly, an independent central bank will always produce better results as long as it is more conservative than the government ( $\lambda^{cb} < \lambda_1^g$ ), irrespective of the latter's commitment to social equality ( $\lambda_2^g$ ).

In deriving our results, we have assumed that the central bank has instrument independence but not target independence. Consequently, the fact that  $EL^g = 0$  can be achieved by setting  $\delta = \lambda^{cb} = 0$  indicates that it is instrument independence which matters; and that target independence is ultimately irrelevant when there is government leadership. Neither target independence nor central bank leadership would reduce society's expected loss to zero (see Appendix 2).

## 6. The Advantage of Government Leadership

### 6.1 Implications of the Theoretical Model

In Hughes Hallett and Weymark (2001), we show that if, in the second stage of

the game, government leadership is removed so that monetary and fiscal policy are implemented simultaneously, then the government's expected loss is given by

$$EL^g = \frac{1}{2} \left\{ \frac{\lambda_1^g}{\alpha} \right\}^2 \left\{ \frac{(\alpha\gamma s)^2}{(\alpha\gamma s)^2 + \phi^2 \lambda_2^g} \right\}. \quad (27)$$

As long as the government has some commitment to social equality (i.e.,  $\lambda_2^g \neq 0$ ), (27) will always be smaller than the loss incurred when government leadership is combined with a dependent central bank .

A more interesting question in this context is whether government leadership with an independent central bank generally produces better outcomes, from society's perspective, than those obtained in the simultaneous move game. In the simultaneous move game, the solution to the government's stage 1 minimization problem is

$$\delta = \frac{\beta\phi^2\lambda^{cb}\lambda_2^g + (\alpha\gamma)^2\beta(\lambda^{cb} - \lambda_1^g)}{\beta\phi^2\lambda^{cb}\lambda_2^g + (\alpha\gamma)^2\beta(\lambda^{cb} - \lambda_1^g) - \phi[\beta\phi + \gamma\Lambda]\lambda_1^g\lambda_2^g}.^8 \quad (28)$$

The optimal degree of conservatism for an independent central bank in this type of game can be obtained by setting  $\delta = 0$  in (28) to yield:

$$\lambda^{cb*} = \frac{(\alpha\gamma s)^2\lambda_1^g}{(\alpha\gamma s)^2 + \phi^2\lambda_2^g} \quad (29)$$

It is straightforward to show that (26) is always less than (27) as long as

$$\lambda^{cb} < [\lambda_1^g\lambda^{cb*}]^{1/2} \quad (30)$$

It is also evident that  $\lambda^{cb*} \leq \lambda_1^g$  for  $\lambda_2^g \geq 0$ . Consequently, government leadership with any  $\lambda^{cb} < \lambda^{cb*}$  will produce better outcomes, from society's point of view, than any simultaneous move game between the central bank and the government.<sup>9</sup> This

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<sup>8</sup>See Weymark (2001) for a full derivation of this result.

<sup>9</sup>Hughes Hallett and Weymark (2001) also show that  $\lambda^{cb*}$  is the critical value that is relevant for comparing government leadership to any simultaneous move regime, including those with  $\delta \neq 0$ . This result follows from the substitutability between  $\delta$  and  $\lambda^{cb}$  in (28).

is an important observation because many inflation targeting regimes, such as those operated by the Bank of England, the Swedish Riksbank, and the Reserve Bank of New Zealand, operate with government leadership; while several others, notably the European Central bank and the US Federal Reserve System, are better characterized as being engaged in a simultaneous move game with their governments.

Substituting  $\delta = 0$  and  $\lambda^{cb}$  into (16)–(18) shows exactly where the advantages of government leadership come from. We get

$$\pi_t = \hat{\pi}, \quad y_t = \frac{-u_t}{\alpha}, \quad \tau_t = \frac{-(b - \theta)u_t}{\alpha} \quad (31)$$

as the final outcomes. By contrast, the optimal outcomes for the associated simultaneous move policy game are

$$\pi_t^* = \hat{\pi} + \frac{\alpha(\gamma s)^2}{[(\alpha\gamma s)^2 + \phi^2\lambda_2^g]} \quad (32)$$

$$y_t^* = \frac{-u_t}{\alpha} \quad (33)$$

$$\tau_t^* = \frac{\gamma s(\lambda^{cb*} - \lambda_1^g)}{\phi\lambda_2^g} - \frac{(b - \theta)u_t}{\alpha} \quad (34)$$

Comparing the two sets of outcomes we see that government leadership eliminates inflationary bias and therefore results in a lower rate of inflation. The optimal outcome under government leadership is also characterized by higher taxes and therefore more income redistribution.<sup>10</sup> Moreover, these improvements in inflation control and income distribution can be achieved with no loss in expected growth.

One of the central issues addressed in the policy coordination literature is whether there are institutional arrangements that yield Pareto improvements over the non-cooperative outcome.<sup>11</sup> When such institutions can be identified, they are viewed as

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<sup>10</sup>Tax revenues are lower under the simultaneous move game because  $\lambda^{cb*} < \lambda_1^g$ . Redistribution is positively related to the amount of tax revenue because  $(b - \theta)Ey_t^* = 0$ , so that  $\tau_t^*$  determines the amount of income redistribution actually achieved.

<sup>11</sup>See, for example, Currie, Holtham, and Hughes Hallett (1989); Currie (1990); and Currie and Levine (1991).



a coordination device. In our model, government leadership in the second stage of the policy game results in better outcomes for both policy authorities and is therefore an example of a rule-based form of policy coordination.<sup>12</sup>

## 6.2 Empirical Evidence

Whether or not the theoretical results we have obtained are of practical significance is an empirical matter. In order to assess the magnitudes of the results we have obtained, we have computed the optimal degrees of conservatism and the associated expected losses under the simultaneous move and government leadership regimes for nine countries. The data we have used is from 1998, which is the year the Eurozone was created. The data itself, and its sources, are summarized in the appendix to this article.

Our sample of countries consists of those which have recently reformed their monetary policy frameworks with the explicit aim of securing lower and more stable inflation rates without damaging the prospects for growth, stability, or social equity. The countries selected fall into three broad groups:

- (a) Eurozone countries: France, Germany, and Italy
- (b) Non-EMU countries with explicit inflation targets: Sweden, Switzerland, and the UK
- (c) Inflation targeters outside the EU: Canada, New Zealand, and the US.

Each of these countries (the US excepted) has revised the statutes and the way in which the central bank is required to conduct monetary policy over the past five to ten years. In each case the creation of an independent central bank (whether fully independent or only instrument independent) has been the key feature of the reforms.

In the first group, monetary policy is conducted at the European level and fiscal policy is conducted independently at the national level. Policy interactions in this group can be characterized in terms of a simultaneous move game with target as well

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<sup>12</sup>See Currie (1990) for a discussion of the distinction between rule-based and discretionary, or *ad hoc*, forms of policy coordination.

TABLE 1

Losses under Government Leadership and Simultaneous Moves

	Full Dependence $\delta = 1$ $\lambda^{cb} = \lambda_1^g$	Government Leadership $\delta = 0$ $\lambda^{cb} = 0$	Simultaneous Moves $\delta = 0$ $\lambda^{cb} = \lambda^{cb*}$	Growth Rate Equivalents Lost %
France	5.78	0.00	0.0125	1.26
Germany	16.14	0.00	0.0079	0.79
Italy	1.28	0.00	0.0116	1.16
Sweden	4.51	0.00	0.0098	0.98
Switzerland	4.79	0.00	0.0251	2.51
UK	3.37	0.00	0.0113	1.13
Canada	12.50	0.00	0.0265	2.65
New Zealand	8.40	0.00	0.0104	1.04
USA	6.47	0.00	0.0441	4.41

as instrument independence. The second group of countries has adopted explicit, and usually publicly announced, inflation targets. Central banks in these countries have been granted a high degree of instrument independence. The government either sets, or helps set, the inflation target value. In each case the government has adopted longer term (supply side) fiscal policies, leaving active demand management to monetary policy. These are clear cases in which there is government leadership, with instrument independent for the central bank.<sup>13</sup> Of the countries in the third group, New Zealand and Canada can also be described as explicit inflation targeters with government leadership. The US, although not an explicit inflation targeter, is included in this group as a point of comparison because of the success with which monetary policy has been employed in the US over the past decade.

The results of our calculations are reported in Table 1. The first column in this

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<sup>13</sup>Switzerland is included in this group on the basis of the inflation targeting changes made after 1999. See Rich (2000) for a detailed analysis of the inflation targeting process in Switzerland.

table shows the losses that would be incurred with a fully dependent central bank; these losses are identical under both regimes. Column two reflects the losses that would be incurred under government leadership with a fully independent central bank that directs monetary policy exclusively towards the achievement of the inflation target (i.e., with  $\delta = \lambda^{cb} = 0$ ). The third column gives the minimum loss associated with simultaneous decision-making in stage two of the policy game.<sup>14</sup>

Evidently, complete dependence is extremely unfavourable for all countries. However, the magnitude of the loss varies considerably from country to country. The losses in column three, relative to those in column 2 appear to be relatively small when measured in terms of raw welfare units. However, when these losses are converted into “growth rate equivalents”, we find that there are significant losses associated with institutional arrangements in which government leadership is absent. The growth rate equivalents reported in the last column of Table 1 were obtained using a standard technique borrowed from the coordination literature.<sup>15</sup> Specifically, we have computed the marginal rates of transformation around each government’s indifference curve to find the change in output growth,  $dy_t$ , that yields the welfare loss given in column four when all other policy variables are held at their optimized values. Formally, we use (7) together with certainty equivalence to obtain

$$dy_t = \frac{(dEL_t^g)}{[\lambda_2^g \{(b - \theta)y_t - \tau_t\} (b - \theta) - \lambda_1^g]}. \quad (35)$$

The minimum value of  $dy_t$  is attained when the tax  $\tau_t$  grows at the same rate as the redistribution target  $(b - \theta)y_t$ . These minimum output losses are reported in column four.

The values in column four show that the losses associated with simultaneous decision-making are equivalent to permanent reductions of 1–2 percent in the long term growth rate of national income. These are significant losses and are roughly

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<sup>14</sup>The losses reported in column 3 were calculated using  $\lambda_1^g = 1$  and  $\lambda_2^g = 0.5$  for each of the countries in the sample as in Hughes Hallett and Weymark (2001).

<sup>15</sup>See, for example, Currie et al (1989), Nolan (2002), and Oudiz and Sachs (1984).

TABLE 2  
Central Bank Conservatism –  $\lambda^{cb}$

	Government Leadership		Simultaneous Moves
	optimal value	upper bound	optimal value
France	0.00	0.0466	0.00217
Germany	0.00	0.0221	0.00049
Italy	0.00	0.0952	0.00906
Sweden	0.00	0.0467	0.00218
Switzerland	0.00	0.0725	0.00525
UK	0.00	0.0579	0.00335
Canada	0.00	0.0458	0.00212
New Zealand	0.00	0.0351	0.00123
USA	0.00	0.0826	0.00682

equivalent to all the gains that might be expected from international policy coordination (Currie et al, 1989), or from introducing the single currency in Europe (EC, 1990).

In Table 1 we have compared the losses associated with government leadership and simultaneous decision-making when the central banking institutions are optimally configured within each regime. However, (30) indicates that the government leadership regime does not need to be optimally configured in order to produce outcomes that are superior to those achieved in the simultaneous move regime. In Table 2, we provide estimates of the lowest degree of central bank conservatism (i.e., the highest value of  $\lambda^{cb}$ ) for which government leadership combined with central bank independence will dominate the optimal simultaneous-move regime. Our calculations show that, compared to the optimal simultaneous-move regime, considerably less central bank conservatism is required to produce good economic outcomes when there is government leadership in policy formation. For Germany, the losses would be lower

under government leadership with  $\lambda^{cb}$  values as much as 50 times larger than under an optimal simultaneous-move regime. In the case of Italy, government leadership is beneficial for  $\lambda^{cb}$  values of up to 10 times larger than under an optimally configured simultaneous-move regime. The remaining six countries fall in between these two extremes. In all cases, the degree of central bank conservatism required under simultaneous decision-making is at least an order of magnitude greater than what is needed when there is government leadership.

The implication of these results is that instrument independence, coupled with government led fiscal policies, allows policy makers a great deal more room for manoeuvre than do regimes that are characterized by a combination of target independence and simultaneous policy moves. Government leadership expands the feasible policy space in that both the central bank and the government can contemplate a wider range of policies to suit their own objectives and still expect to get better outcomes, from society's point of view, than in other regimes. Conversely, a government leadership regime is likely to be less sensitive to any variations in the transmission parameters, savings ratios, or targets for social equality that may appear around the economic cycle, or as new governments come into office. This last point may prove to be the greater advantage in practical applications.

## 7. Conclusion

In this article, we have developed a model of monetary delegation in which the government plays a leadership role. We find that when the government has the first-mover advantage in formulating fiscal policy, society's well-being (as we have defined it) is maximized by appointing a central banker whose only concern is the achievement of the government-mandated inflation target.

Our theoretical results show that government policy leadership, coupled with a fully independent, inflation-oriented central bank, will lead to a better economic performance, from society's point of view, than a simultaneous move game between the central bank and the government. In comparing the optimal economic outcomes that

can be achieved under each of the two regimes, we find that government leadership results in Pareto improvements across all objectives for all players. This suggests that the improved outcomes obtained under government leadership come from the greater (implicit) coordination that this regime generates between the two independent policy authorities.

Our empirical analysis indicates that the benefits of government leadership are large enough to allow policy makers to achieve good outcomes with a much wider range of policies than in the simultaneous move regime. Moreover, because the success of the leadership regime is less sensitive to the precise choice of the degree of conservatism, it provides some protection against the impact of variations in transmission parameters or social objectives on economic outcomes. Our results are of particular significance for countries like the UK and Sweden, who must decide whether the benefits of joining the European Monetary Union are sufficient to justify the cost of giving up monetary sovereignty and government leadership in policy formation.

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## Appendix 1

### Solutions to (22) and (23)

The first-order condition (23) can be written as a quartic polynomial in  $\delta$ . As a consequence, there are four solutions that simultaneously satisfy (22) and (23). By inspection, it is apparent that one of these solutions is  $\delta = 1$  and  $\lambda^{cb} = \lambda_1^g$ . When  $\delta \neq 1$  and  $\lambda^{cb} \neq \lambda_1^g$ , the first order conditions can be written

$$\begin{aligned} (\phi - \eta\Lambda)\lambda_2^g \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \\ - (1 - \delta)(\beta\eta + \gamma)^2(\alpha s)^2\beta(\lambda_1^g - \lambda^{cb}) = 0 \end{aligned} \quad (\text{A.1})$$

$$\begin{aligned} \left[ \delta(1 - \delta)\Lambda\frac{\partial\eta}{\partial\delta} + (\phi - \eta\Lambda) \right] \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \lambda_2^g \\ - (1 - \delta)(\beta\eta + \gamma)(\alpha s)^2\beta \left[ (\beta\eta + \gamma) - (1 - \delta)\beta\frac{\partial\eta}{\partial\delta} \right] (\lambda_1^g - \lambda^{cb}) = 0. \end{aligned} \quad (\text{A.2})$$

But (A.2) can be expressed as

$$\begin{aligned} (\text{A.1}) + \delta(1 - \delta)\Lambda\frac{\partial\eta}{\partial\delta} \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \lambda_2^g \\ + (1 - \delta)^2(\beta\eta + \gamma)\frac{\partial\eta}{\partial\delta}(\alpha\beta s)^2(\lambda_1^g - \lambda^{cb}) = 0. \end{aligned} \quad (\text{A.3})$$

Consequently, when  $\delta \neq 1$  and (A.1) is satisfied, (A.2) becomes

$$\begin{aligned} \delta\Lambda \left\{ (1 - \delta)\beta(\phi - \eta\Lambda)\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \lambda_2^g \\ + (1 - \delta)(\beta\eta + \gamma)(\alpha\beta s)^2(\lambda_1^g - \lambda^{cb}) = 0. \end{aligned} \quad (\text{A.4})$$



Replacing  $\eta$  with (13) yields

$$(\phi - \eta\Lambda) = \frac{\alpha^2\beta s^2[\beta\phi + \gamma\Lambda]}{(\alpha\beta s)^2 + \delta\Lambda^2\lambda_2^g} \quad \text{and} \quad (\beta\eta + \gamma) = \frac{\delta\Lambda[\beta\phi + \gamma\Lambda]\lambda_2^g}{(\alpha\beta s)^2 + \delta\Lambda^2\lambda_2^g}. \quad (\text{A.5})$$

It is evident that  $(\beta\eta + \gamma) = 0$  when  $\delta = 0$ . Hence  $\delta = \lambda^{cb} = 0$  is one solution that satisfies (A.1) and (A.4).

The remaining potential solutions can be found by substituting (A.5) into (A.4) and solving for  $\delta$  (under the assumption that  $\delta \neq 0$  and  $\delta \neq 1$ ). We obtain:

$$\delta^2 = \frac{-(\alpha\beta s)^2}{\Lambda^2\lambda_1^g\lambda_2^g}. \quad (\text{A.6})$$

Consequently, there are only two real-valued solutions that satisfy the first-order necessary conditions: (i)  $\delta = 1$  and  $\lambda^{cb} = \lambda_1^g$ , and (ii)  $\delta = \lambda^{cb} = 0$ .

## Appendix 2

### Central Bank leadership

This appendix summarizes the results obtained when the central bank, rather than the government, is the Stackelberg leader in the second stage of the policy game. Because a central bank that plays a leadership role is almost certain to have target independence, we express the objectives of the central bank as follows:

$$L_t^{cb} = \frac{1}{2}(\pi_t - \hat{\pi}^{cb})^2 - (1 - \delta)\lambda^{cb}y_t - \delta\lambda_1^g y_t + \frac{\delta\lambda_2^g}{2}[(b - \theta)y_t - \tau_t]^2 \quad (\text{A.7})$$

where we allow the central bank's inflation target  $\hat{\pi}^{cb}$  to differ from the government's inflation target  $\hat{\pi}$ .

When the central bank has full target independence and is the Stackelberg leader, the reduced-form solutions for  $\pi_t$ ,  $y_t$ , and  $\tau_t$  are:

$$\begin{aligned} \pi_t = & \frac{[(\beta + \mu\gamma)\phi\hat{\pi}^{cb} + \delta\gamma(\Lambda - \mu\phi)\hat{\pi}]}{(\beta + \mu\gamma)\phi + \delta\gamma(\Lambda - \mu\phi)} + \frac{(1 - \delta)(\beta + \mu\gamma)\phi\lambda^{cb}}{\alpha[(\beta + \mu\gamma)\phi + \delta\gamma(\Lambda - \mu\phi)]} \\ & + \frac{\delta[\beta\phi + \gamma\Lambda]\lambda_1^g}{\alpha[(\beta + \mu\gamma)\phi + \delta\gamma(\Lambda - \mu\phi)]} \end{aligned} \quad (\text{A.8})$$

$$y_t = \frac{-u_t}{\alpha} \quad (\text{A.9})$$

$$\begin{aligned} \tau_t = & \frac{\alpha\gamma s(\beta + \mu\gamma)(\hat{\pi} - \hat{\pi}^{cb})}{[(\beta + \mu\gamma)\phi + \delta\gamma(\Lambda - \mu\phi)]\lambda_2^g} \\ & + \frac{(1 - \delta)\gamma(\beta + \mu\gamma)s(\lambda_1^g - \lambda^{cb})}{[(\beta + \mu\gamma)\phi + \delta\gamma(\Lambda - \mu\phi)]\lambda_2^g} - \frac{(b - \theta)u_t}{\alpha} \end{aligned} \quad (\text{A.10})$$

$$\text{where } \mu = \frac{\partial g_t}{\partial m_t} = \frac{-\alpha^2\beta\gamma s^2 + \phi\Lambda\lambda_2^g}{(\alpha\gamma s)^2 + \phi^2\lambda_2^g}.$$

Substituting (A.8)–(A.10) into the government's loss function (7) and differentiating with respect to  $\lambda^{cb}$  and  $\delta$  yields the necessary first-order conditions:

$$\begin{aligned} \frac{\partial EL_t^g}{\partial \lambda^{cb}} &= 0 \\ \Rightarrow & (1 - \delta)\phi\lambda_2^g \left\{ -\alpha\Gamma\phi(\hat{\pi} - \hat{\pi}^{cb}) + \phi(1 - \delta)\Gamma\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \\ & - (\alpha\gamma s)^2\Gamma(1 - \delta) \left[ \alpha(\hat{\pi} - \hat{\pi}^{cb}) + (1 - \delta)(\lambda_1^g - \lambda^{cb}) \right] = 0 \end{aligned} \quad (\text{A.11})$$

$$\begin{aligned} \frac{\partial EL_t^g}{\partial \lambda^{cb}} &= 0 \\ \Rightarrow & \phi\lambda_2^g\Gamma\Sigma \left\{ -\alpha(\beta + \mu\gamma)\phi(\hat{\pi} - \hat{\pi}^{cb}) + \phi(1 - \delta)\Gamma\lambda^{cb} + \delta[\beta\phi + \gamma\Lambda]\lambda_1^g \right\} \\ & - (\alpha\gamma s)^2\Gamma^2\Sigma \left[ \alpha(\hat{\pi} - \hat{\pi}^{cb}) + (1 - \delta)(\lambda_1^g - \lambda^{cb}) \right] = 0 \end{aligned} \quad (\text{A.12})$$

where

$$\begin{aligned} \Sigma &= [\beta\phi + \gamma\Lambda](\lambda_1^g - \lambda^{cb}) + \alpha\gamma(\hat{\pi} - \hat{\pi}^{cb})(\Lambda - \mu\phi) \\ \Gamma &= (\beta + \mu\gamma). \end{aligned}$$

There are two solutions that satisfy both of the first-order conditions given above. By inspection, it is apparent that (A.11) and (A.12) are both satisfied when  $\delta = 1$  and  $\Gamma = 0$ . When  $0 \leq \delta < 1$  and  $\Gamma \neq 0$ , then (A.11) and (A.12) imply the following relationship between  $\delta$  and  $\lambda^{cb}$

$$\delta = \frac{(\beta + \mu\gamma) \left\{ \phi^2\lambda^{cb}\lambda_2^g + (\alpha\gamma s)^2(\lambda^{cb} - \lambda_1^g) - \alpha[\phi^2\lambda_2^g + (\alpha\gamma s)^2](\hat{\pi} - \hat{\pi}^{cb}) \right\}}{(\beta + \mu\gamma) \left\{ \phi^2\lambda^{cb}\lambda_2^g + (\alpha\gamma s)^2(\lambda^{cb} - \lambda_1^g) \right\} - \phi[\beta\phi + \gamma\Lambda]\lambda_1^g\lambda_2^g}. \quad (\text{A.13})$$

It is straightforward to show that the government’s expected losses are minimized by combinations of  $\delta$  and  $\lambda^{cb}$  that satisfy (A.13). Substituting (A.13) into the right-hand-side of (19) then yields

$$EL^g = \frac{(\lambda_1^g)^2}{2\alpha^2} \left\{ \frac{(\alpha\gamma s)^2}{(\alpha\gamma s)^2 + \phi^2\lambda_2^g} \right\}. \quad (\text{A.14})$$

Comparing (A.15) with (25) shows that the government’s (and society’s) expected loss is greater under central bank leadership than under government leadership. In fact, the loss under central bank leadership is identical to the loss incurred by the government in a simultaneous move regime. Furthermore, target independence has no impact on economic outcomes or government losses as long as the government can alter the degree of central bank conservatism to compensate for the difference between its own inflation target and that of the central bank. To see this, note that when the central bank is fully independent (i.e.,  $\delta = 0$ ), the optimal degree of central bank conservatism (from A.13) is given by

$$\lambda^{cb} = \frac{(\alpha\gamma s)^2\lambda_1^g}{(\alpha\gamma s)^2 + \phi^2\lambda_2^g} + \alpha(\hat{\pi} - \hat{\pi}^{cb}). \quad (\text{A.15})$$

## Appendix 3

### Data Sources and Parameter Values

The parameter values used in Section 6 are set out in Table 3. They come from different sources, and are offered as “best practice” estimates of the relevant parameters for a stylized facts analysis. The advantages of further econometric refinements, or consistency constraints on the underlying econometric specifications, would be lost if we varied the parameter values to capture the effects of different preference or transmission asymmetries on performance.

The Phillips curve parameter,  $\alpha$  from (1), is the inverse of the annualized sacrifice ratios estimated on quarterly data from 1971-1998 by Turner and Seghezza (1999).<sup>16</sup>

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<sup>16</sup>Turner and Seghezza (1999) also note that there is no significant difference between the numerical estimates obtained from single-country estimation and OECD-wide systems estimation. This justifies our use of single country estimates in (1)-(3) for economies that are subject to spillover effects.

TABLE 3  
Country-Specific Parameter Values

	$\alpha$	$\beta$	$\gamma$	$s$	$\theta$	$\phi$
France	0.294	0.500	0.57	0.211	0.620	1.072
Germany	0.176	0.533	0.43	0.216	0.583	1.040
Italy	0.625	0.433	0.60	0.214	0.651	1.187
Sweden	0.333	0.489	0.533	0.206	0.504	1.107
Switzerland	0.323	0.489	0.533	0.3310	0.719	1.039
UK	0.385	0.133	0.58	0.180	0.675	0.980
Canada	0.200	0.400	0.850	0.185	0.725	0.966
New Zealand	0.244	0.400	0.850	0.124	0.596	1.035
US	0.278	0.467	1.150	0.184	0.597	1.004

From (2),  $\beta$  and  $\gamma$  measure the effectiveness of monetary and fiscal policy, respectively. We obtained the  $\beta$  and  $\gamma$  values used in Tables 1 and 2 from John Taylor's (1993) multicountry econometric model; they are the simulated one-year policy multipliers for each economy, jointly estimated in a model of interdependent economies. Thus, although our model (1)-(3) does not make spillovers between economies explicit, our numerical estimates do reflect the performance of an economy subject to such spillovers.

The national savings ratios  $s$  were obtained from OECD data (Economic Outlook, various issues). We chose to use 1998 data because that was the year in which EMU started. We also used 1998 OECD data to estimate the desired level of income equality  $\theta$ . According to our model,  $\theta$  measures the desired degree of income equality in terms of the desired proportion of output allocated to the rich. We therefore estimate  $\theta$  as one minus the proportion of total fiscal expenditure allocated to social expenditures in each country.

Finally,  $\lambda_1^g$  and  $\lambda_2^g$  represent the  $i$ th country's preference for growth and income redistribution, respectively, relative to a unit penalty for inflation aversion. For lack of

any direct evidence on these preference parameters, we have set  $\lambda_1^g = 1$  and  $\lambda_2^g = 0.5$ , for each country in the sample.